

Space charge calculations

May 02 2016

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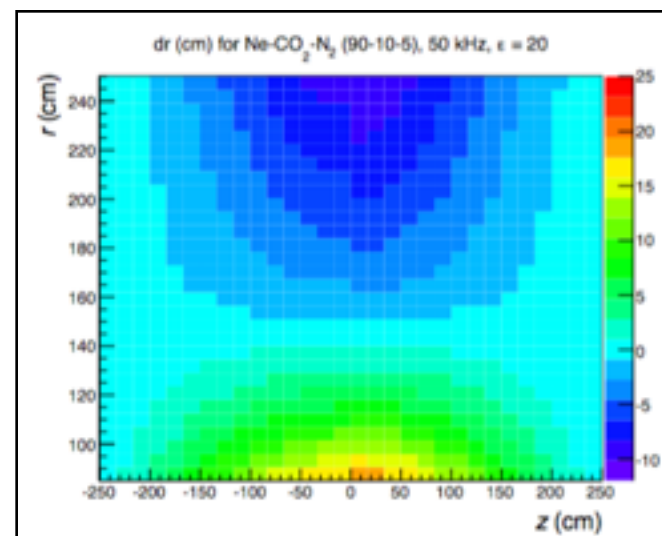
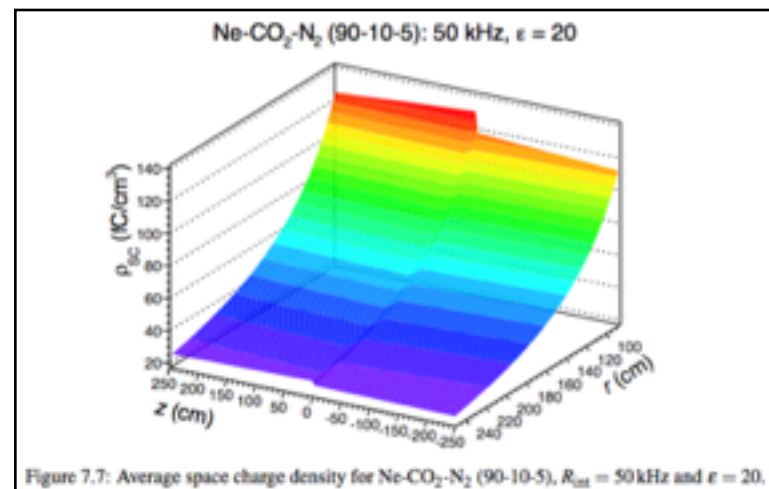
Outlook:

- R-Distortions ALICE/PHENIX
- Charge density from FP

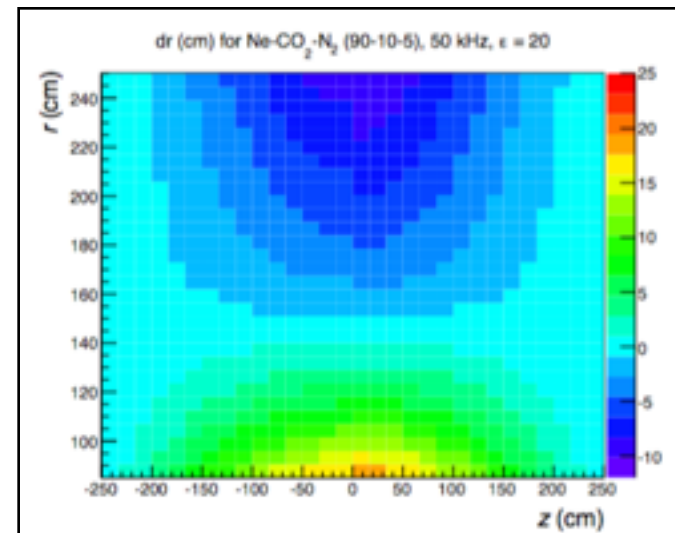
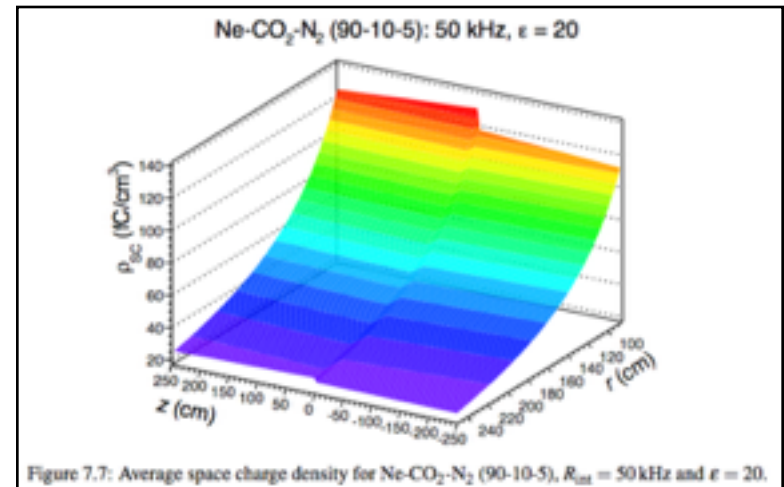
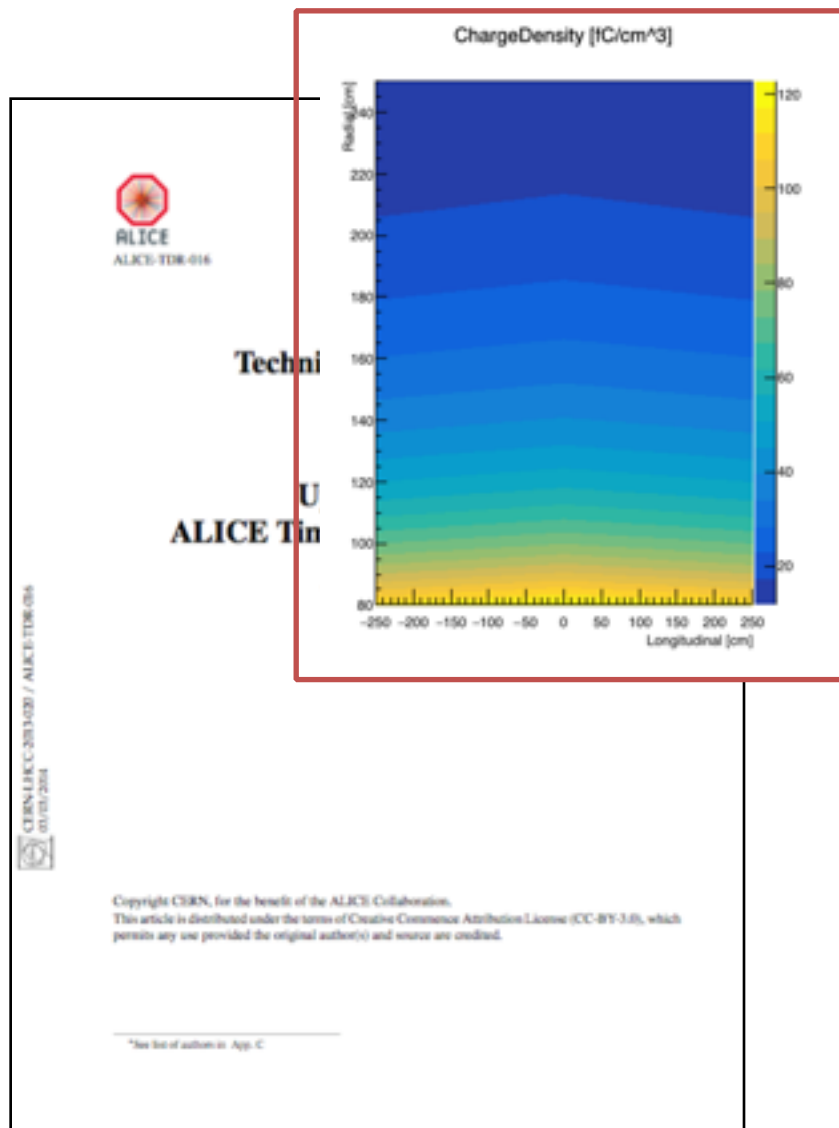
Methodology for distortions

- Initial Charge Density [toy model (ala ALICE)]
- E_r and E_z from Laplace solution to ICD in cage at $V=0$
- ΔR from Langevin formalism using $E_z = 400\text{V/cm}$

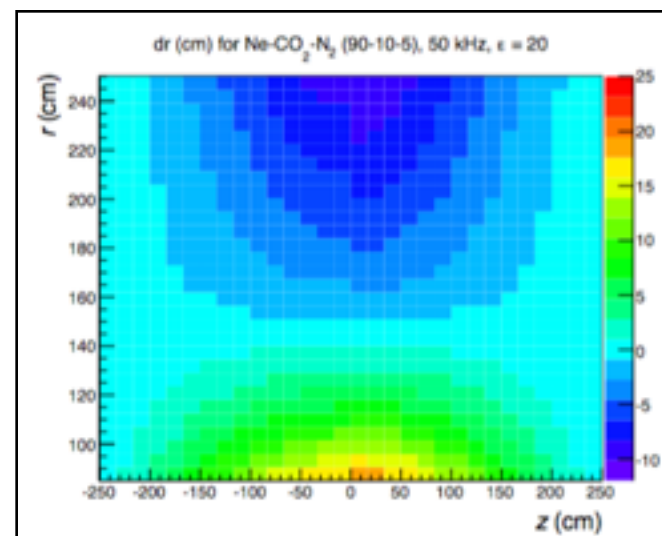
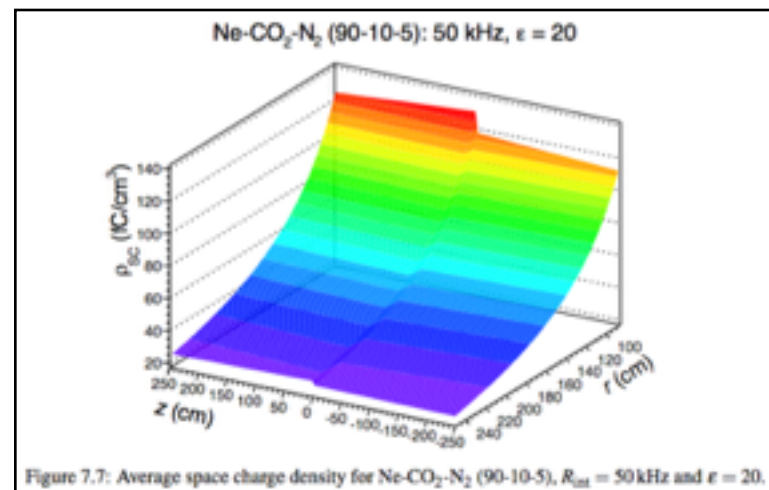
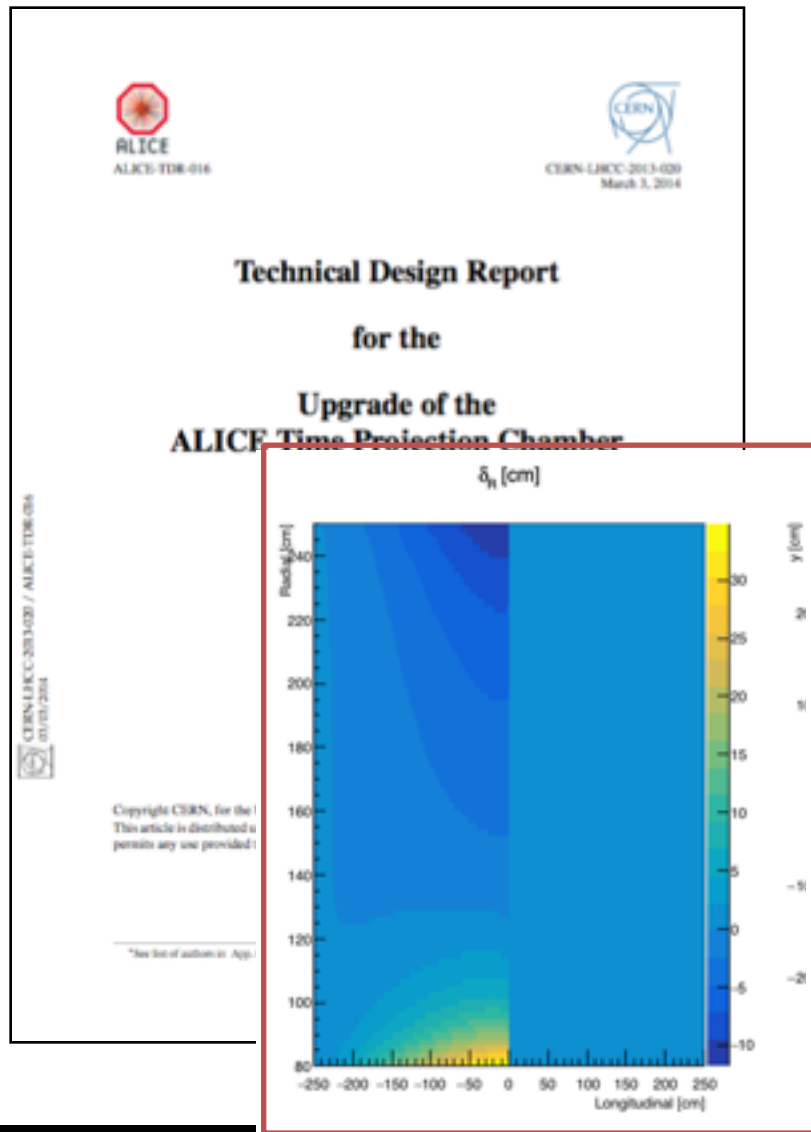
ALICE reproduction



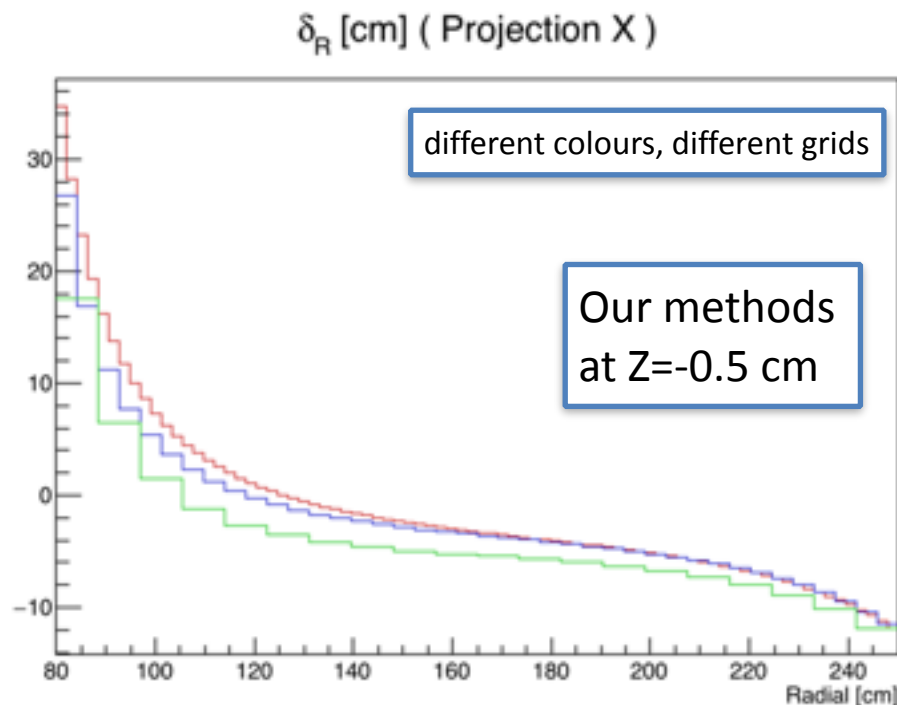
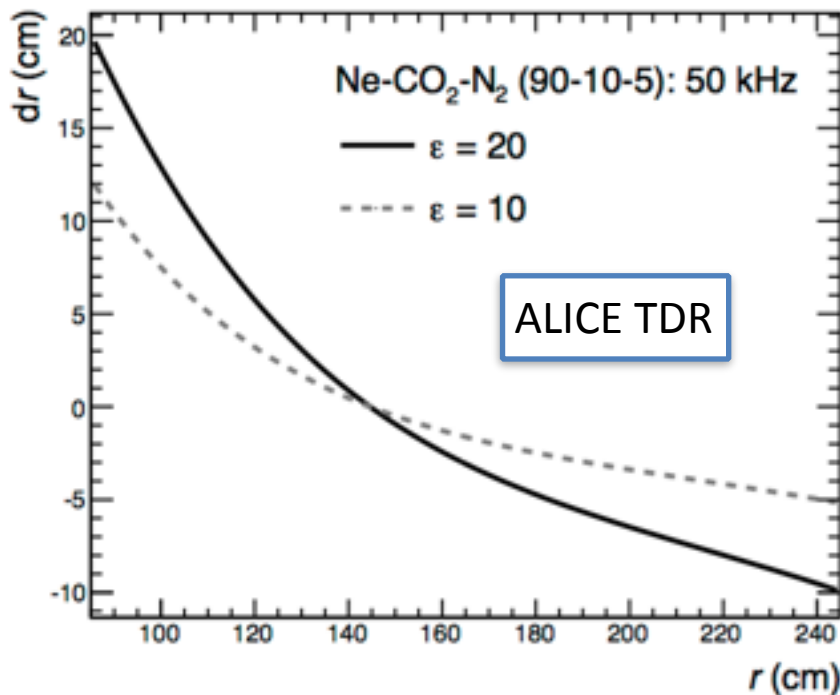
ALICE reproduction



ALICE reproduction



Dr detailed shape comparison



Quantitatively close, but not quite the right shape

Source of incongruence:

- We do Laplace expansion up to 15th order (ALICE claims 30th)
- We use $E_z = E_0 + dE_z$ (ALICE does not say)
- We probe Dr at $z = -0.5$ cm (ALICE gets it at $z = 0.5$)
- We use $1/r^2$ in ICD (ALICE claims $1/r^{1.5}$)
- ...?

Estimated mean distortions in R

ALICE

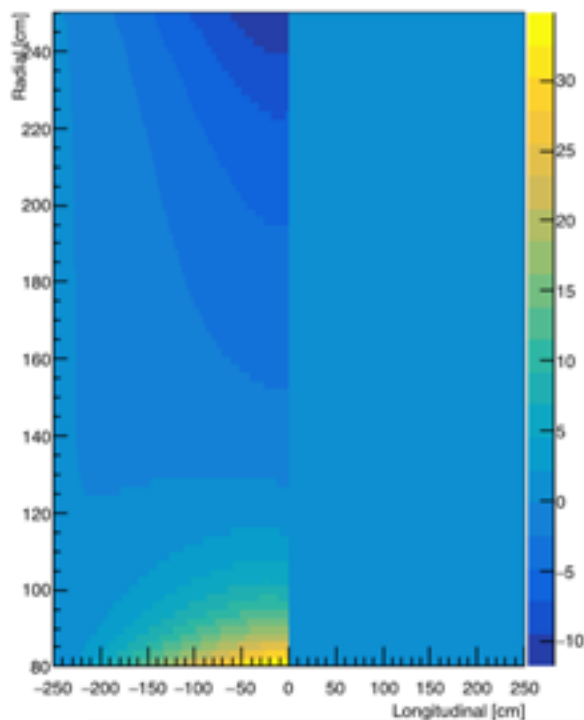
Grid size:

Rad = 2.13 cm

Phi = 360 deg

Lon = 2 cm

δ_R [cm]



sPHENIX20

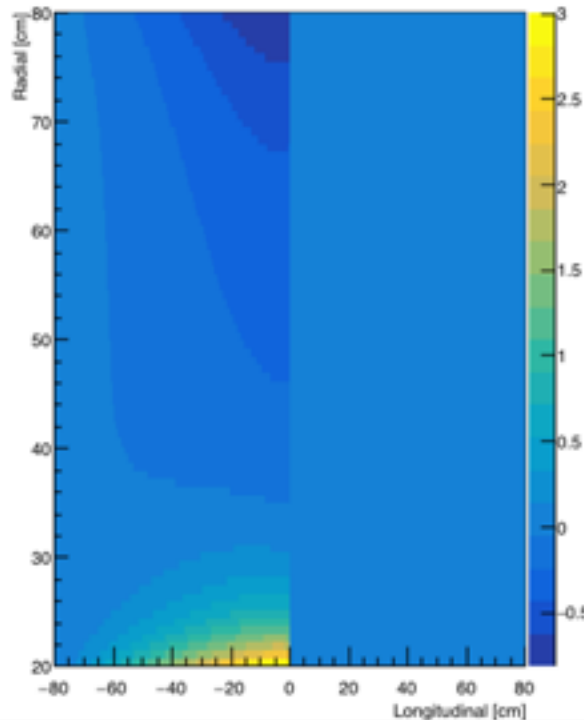
Grid size:

Rad = 0.75 cm

Phi = 360 deg

Lon = 0.64 cm

δ_R [cm]



sPHENIX30

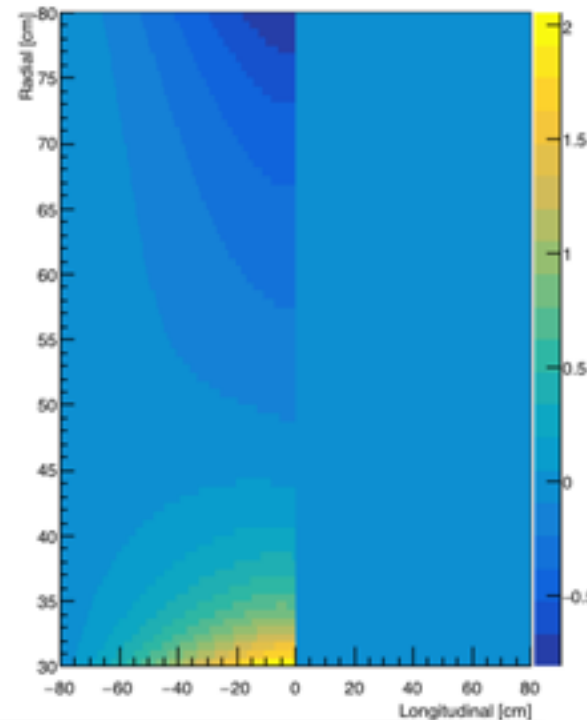
Grid size:

Rad = 0.63 cm

Phi = 360 deg

Lon = 0.64 cm

δ_R [cm]



Gas parameters left alike, mean multiplicity scaled by a factor ~ 2 compared to ALICE

Estimated mean distortions in R

ALICE

Grid size

Rad =

Phi = 3

Lon =

sPHENIX20

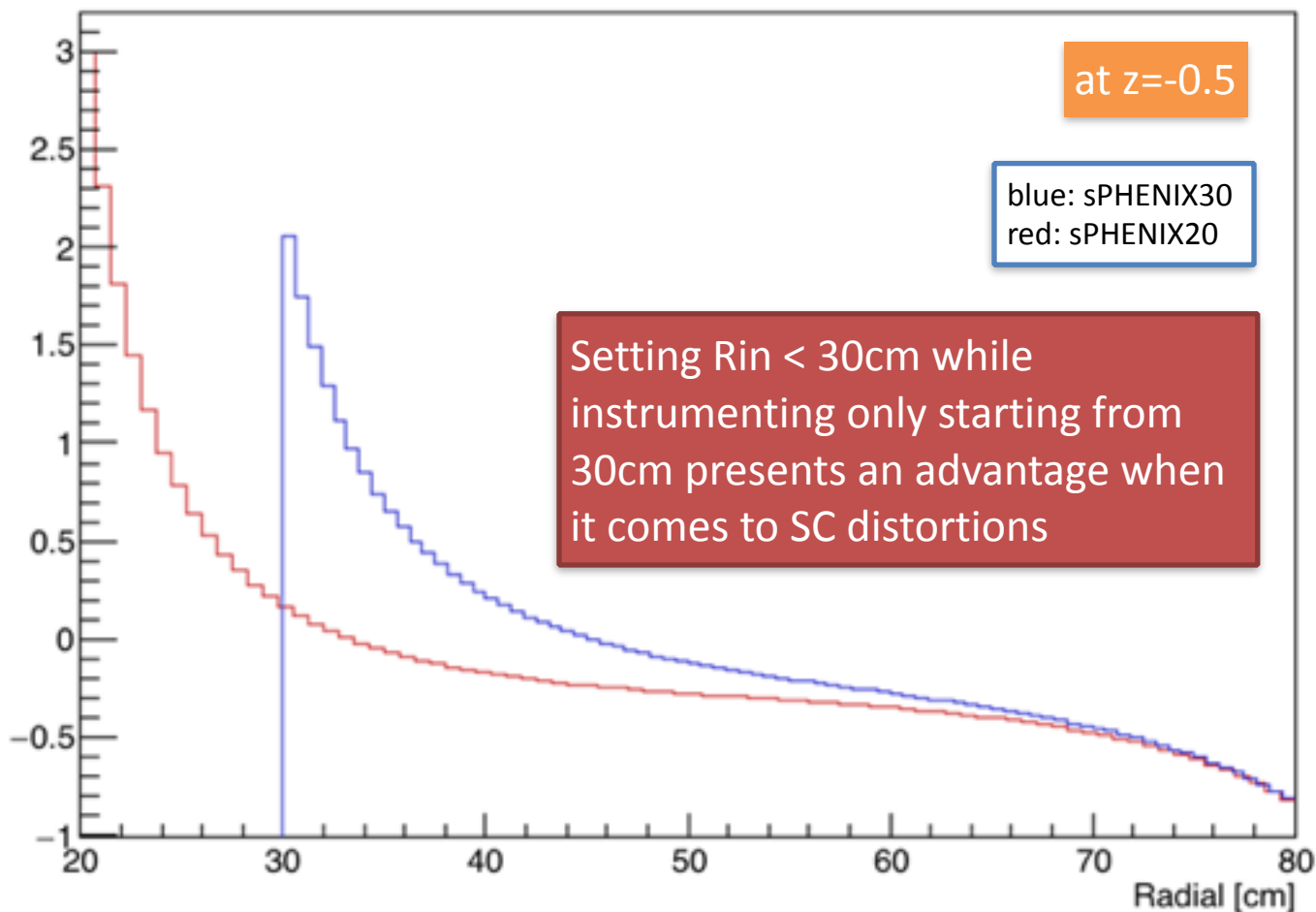
sPHENIX30

δ_R [cm] (Projection X)

at $z=-0.5$

blue: sPHENIX30
red: sPHENIX20

Setting $R_{in} < 30\text{cm}$ while instrumenting only starting from 30cm presents an advantage when it comes to SC distortions



More on Initial Charge Density

- Initial Charge Density was modelled so far using phenomenological expression from ALICE/STAR
- Many control variables like “gas factor”, “multiplicity”, “ion-feedback” are used heuristically.
- To gain full control on the gas response and realistic track density, it is desirable to model this from First Principles.

Very preliminary

Algorithm Flow chart

ChargeMap(X)

1. Contains list of ions/electrons in TPC

RecordTime

Event

1. Generate particles (X,P)
2. Particles \rightarrow helix traces
3. traces \rightarrow electron - ion
4. pushes new pairs into "ChargeMap"

Pythia / HIjing

Transport

1. Evolves ChargeMap in lapse between events

Parameters used

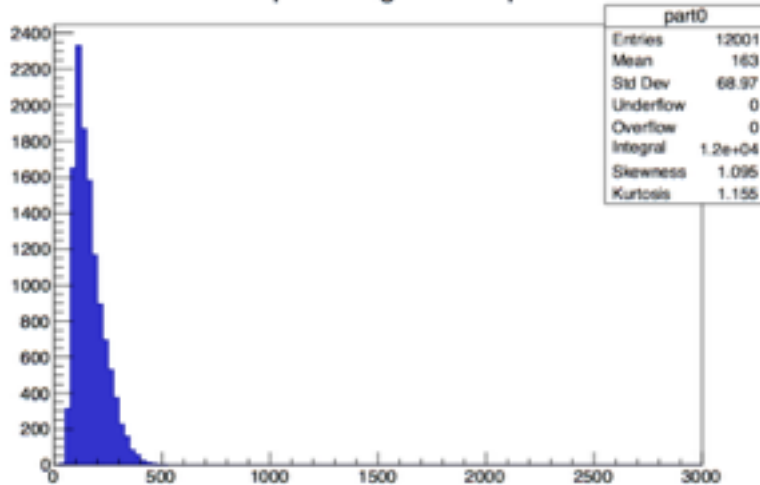
```
//=====
// Gas parameters
float gs_nt = 47.80; // [cm-1]
float gs_ion_mobility = 4; // [cm2/(V.s)]

//=====
// TPC running conditions
float tpc_magnetic_field = 1.5; // [Tesla]
float tpc_electric_field = 400; // [V/cm]
float tpc_drift_velocity_e = 8; // [cm/us]
float tpc_drift_velocity_i = tpc_electric_field*gs_ion_mobility*1e-3; // [cm/ms]
float tpc_readout_rate = 50; // [kHz]
```

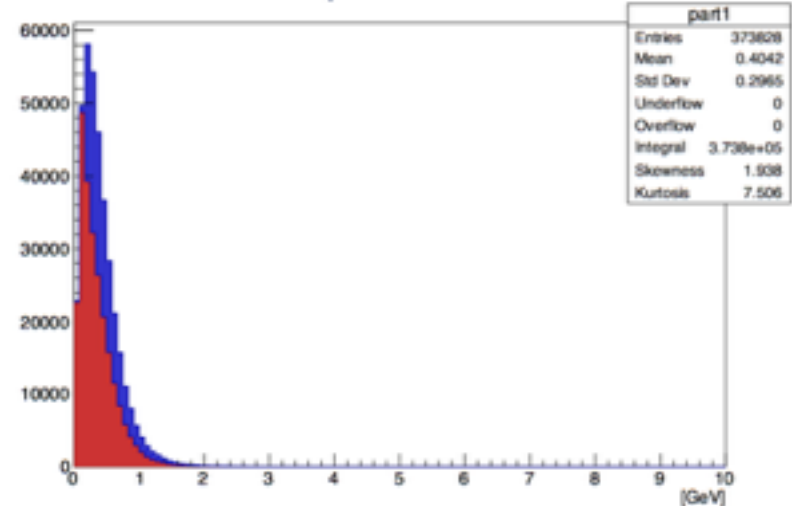
TPC dimensions: Rad = [30,80] cm | Length = 2 x 80cm

Pythia8: 12k events PP@200 GeV

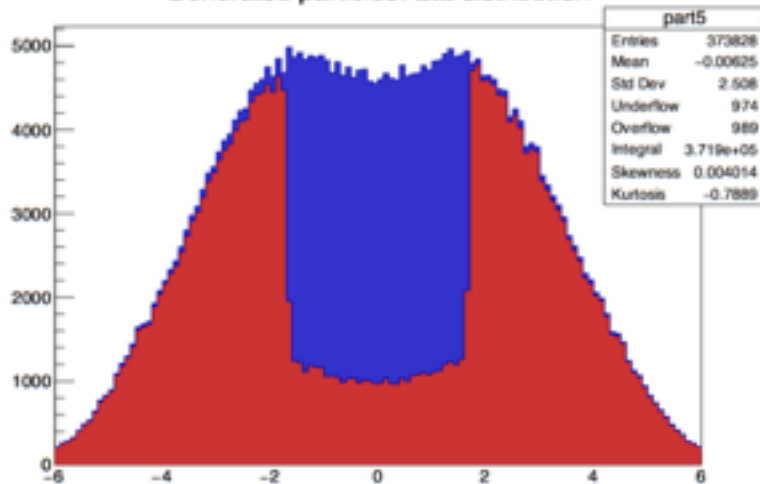
Number Of particles generated per event



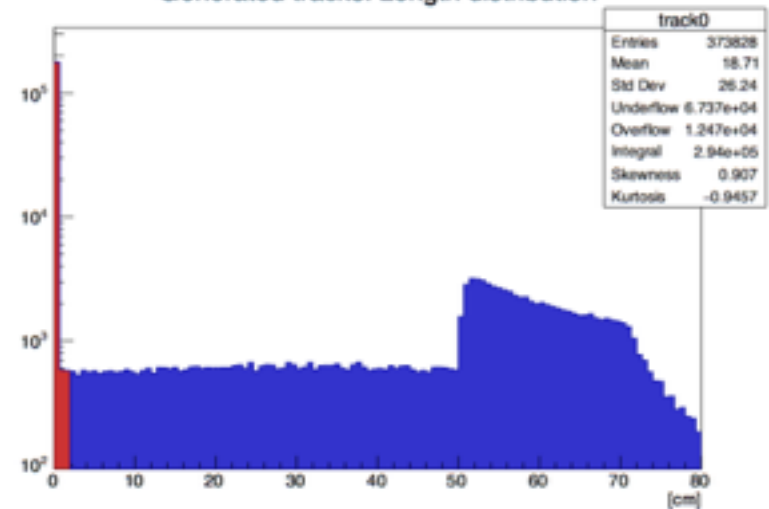
Generated particles: Pt distribution



Generated particles: Eta distribution



Generated tracks: Length distribution



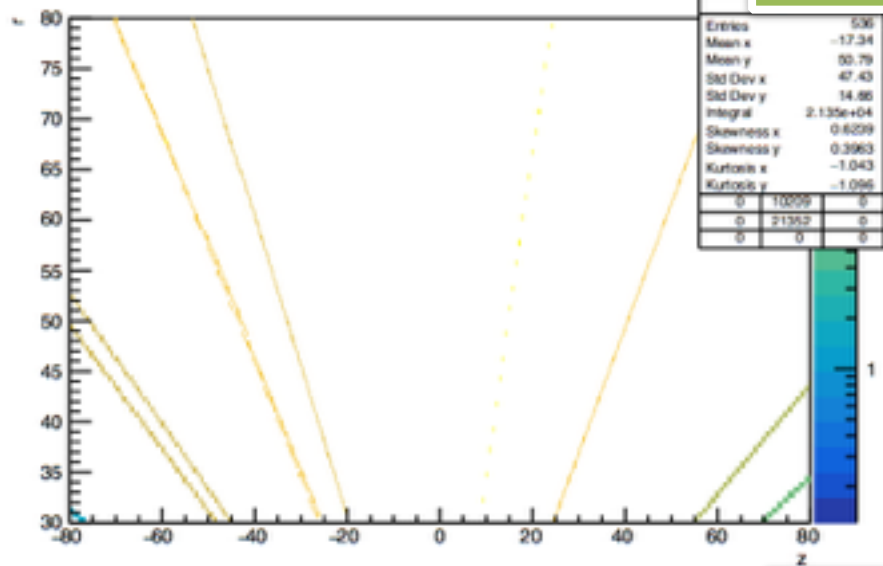
Frame set to minimum
ion displacement

First two events

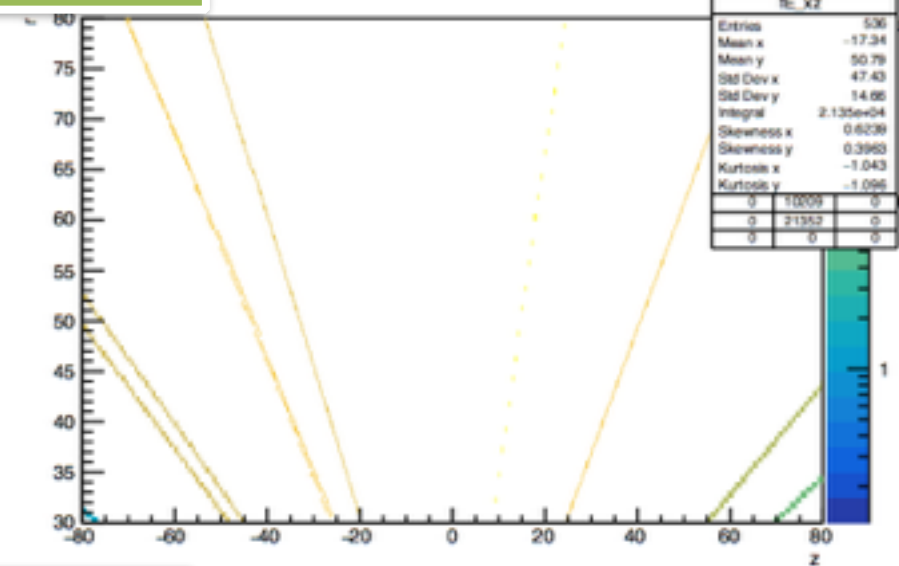
using back flow 1%

Before propagation

IonMap (ev==0)

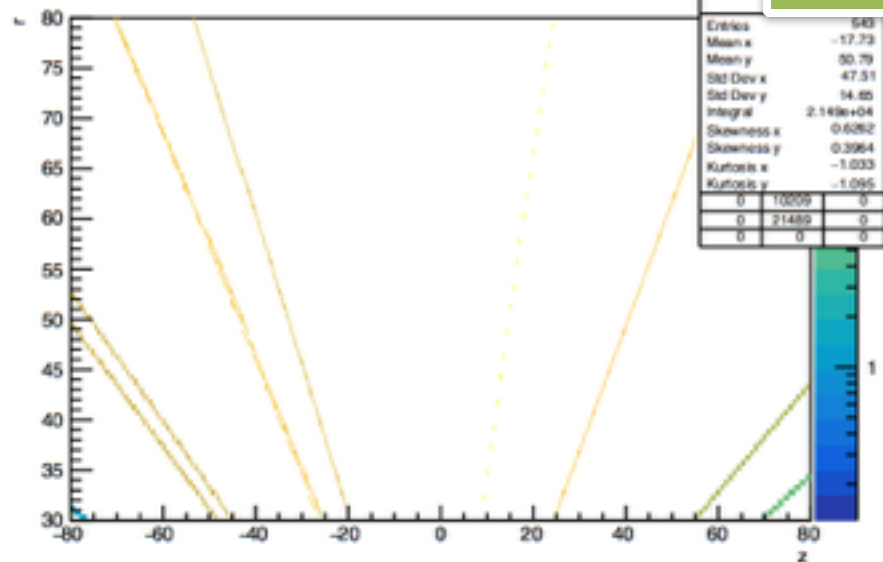


ElectronMap (ev==0)

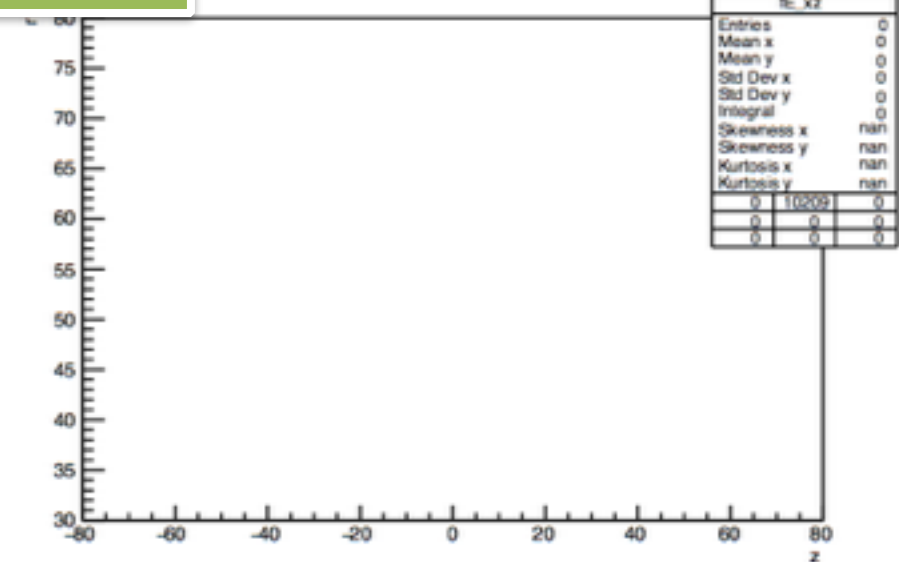


After propagation

IonMap (ev==0)



ElectronMap (ev==0)



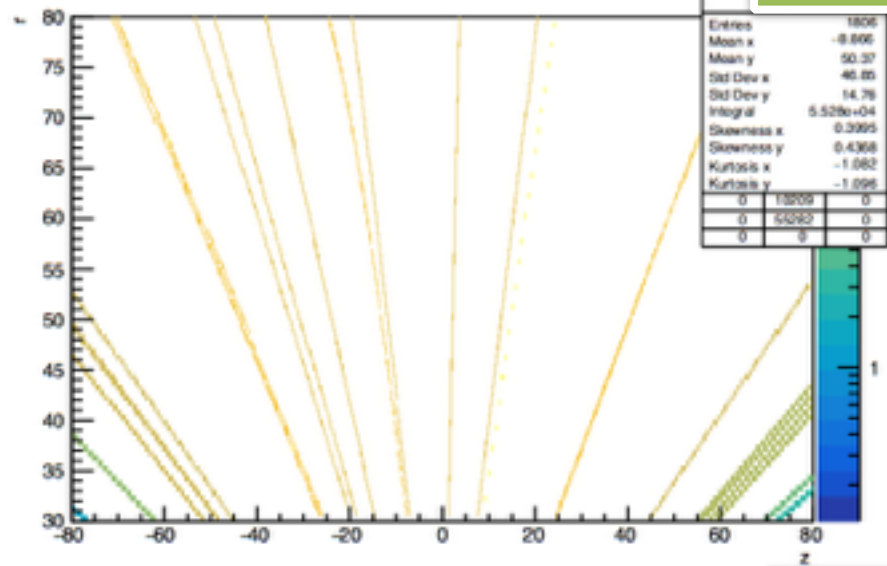
Frame set to minimum
ion displacement

First two events

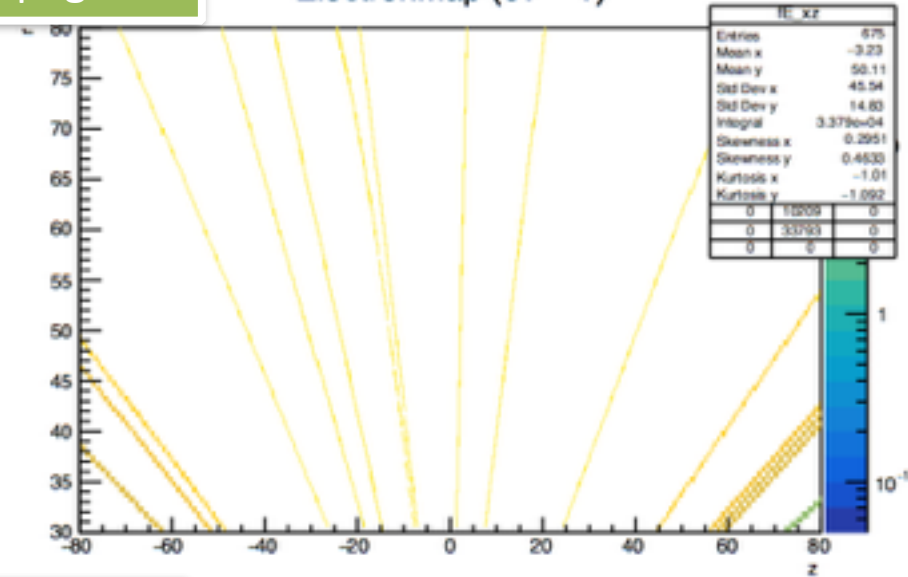
using back flow 1%

Before propagation

IonMap (ev==1)

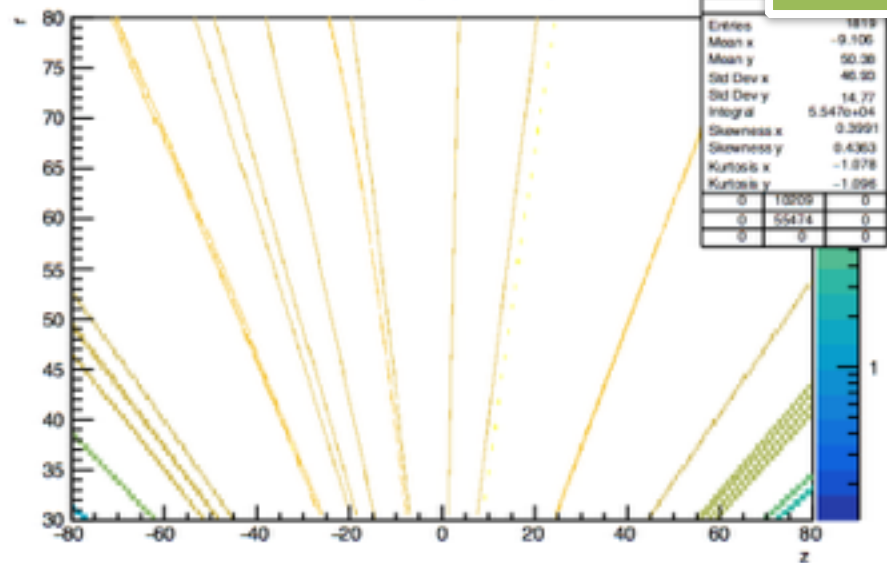


ElectronMap (ev==1)

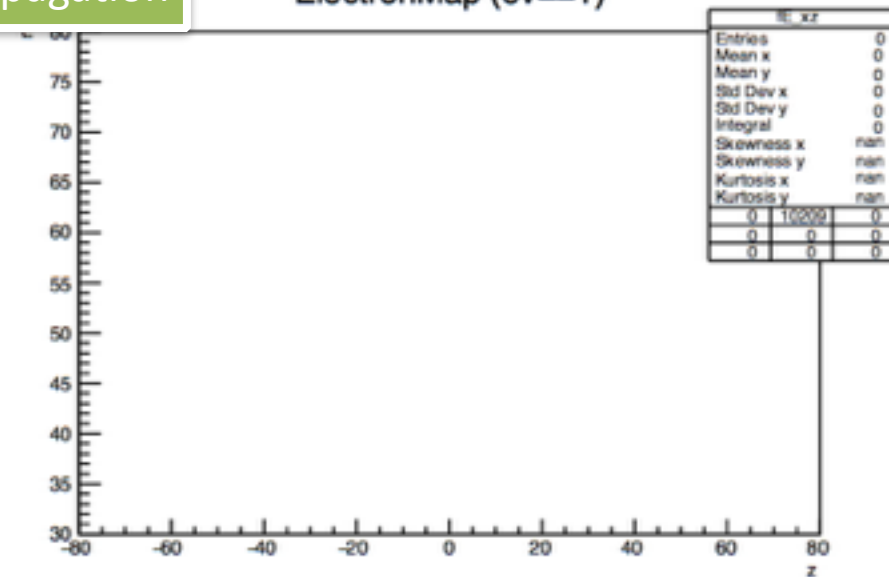


After propagation

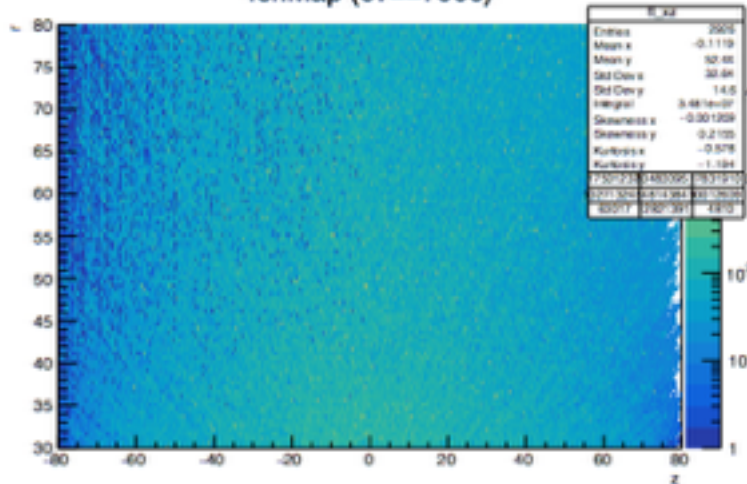
IonMap (ev==1)



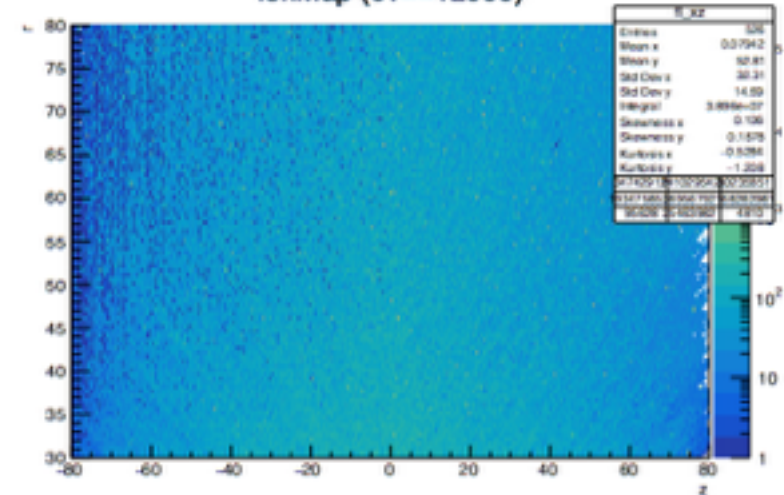
ElectronMap (ev==1)



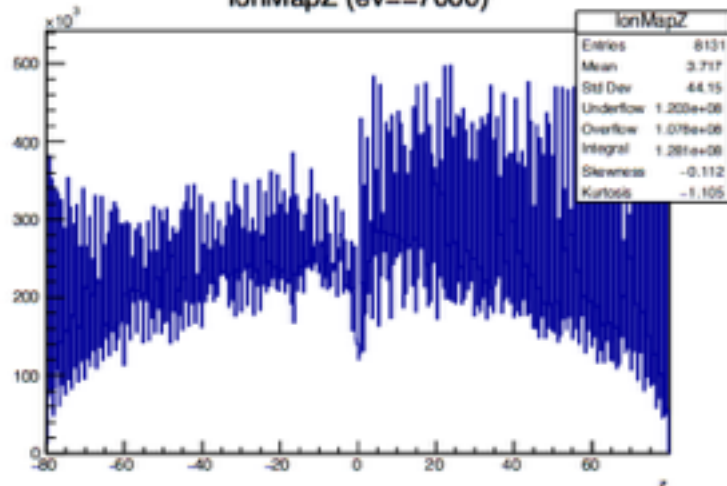
IonMap (ev==7000)



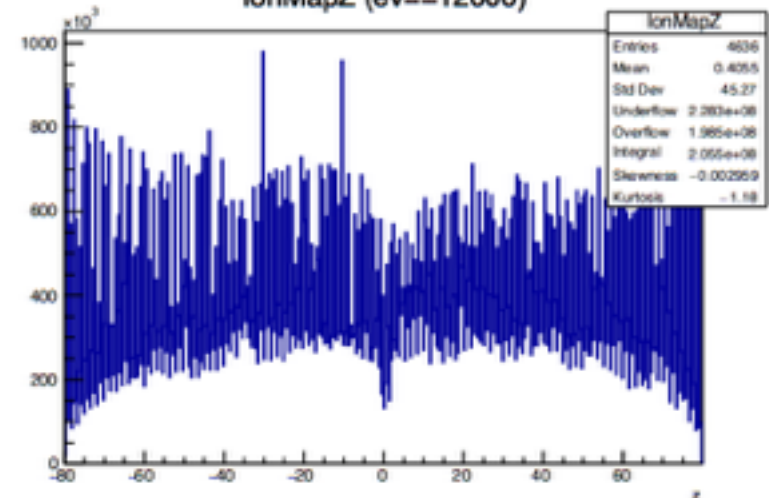
IonMap (ev==12000)



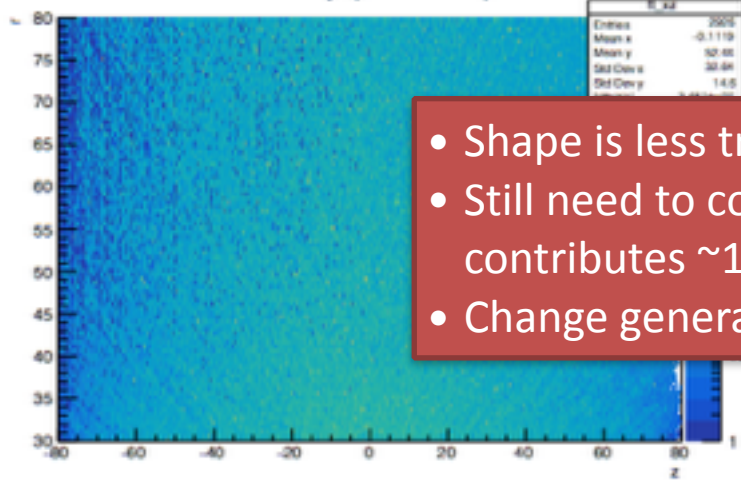
IonMapZ (ev==7000)



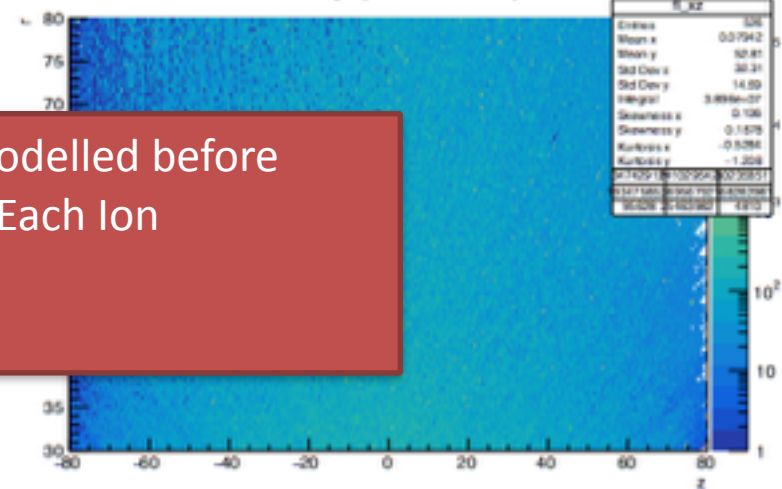
IonMapZ (ev==12000)



IonMap (ev==7000)

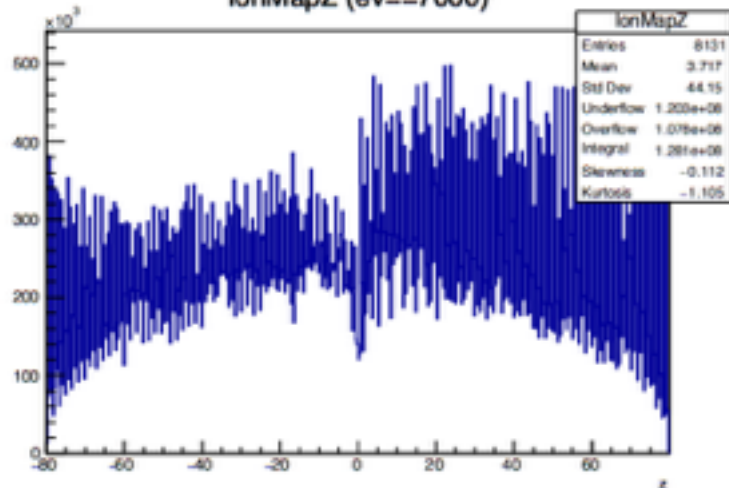


IonMap (ev==12000)

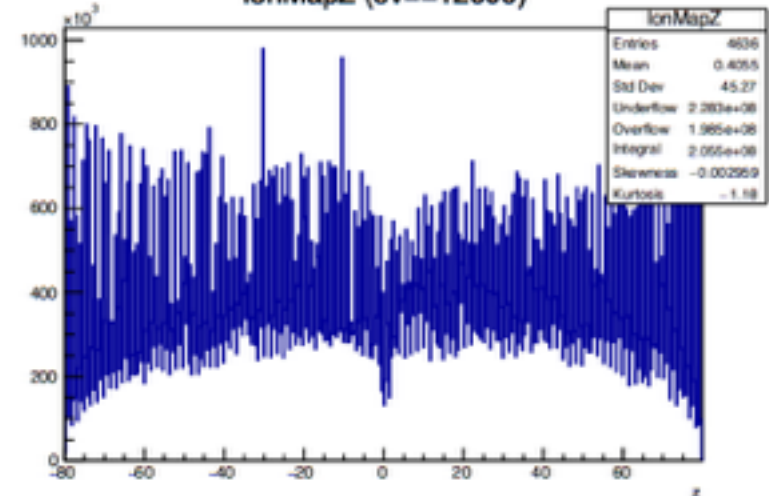


- Shape is less triangular than modelled before
- Still need to compute density (Each Ion contributes $\sim 1.6 \times 10^{-4}$ fC)
- Change generator for AuAu

IonMapZ (ev==7000)



IonMapZ (ev==12000)



BACKUP

Space charge density for STAR

$$\rho(r_-, z_-) := A \left(\frac{1 - b z + c \epsilon}{f_d r^d} \right)$$

- Inner radius = 50 cm, Outer radius = 200 cm, Longitudinal length = 210 cm, $\phi = 2\pi$

ALICE has this factor named "empirical factor" quoted as 76628

Derivation for ALICE from STAR

- $A = [G] \times [m] \times [r] \times [e_0] / 19318. \text{ [in C/m]}$
 - $e_0 (=8.85e-12)$: vacuum permittivity
 - $G = 1$
 - M : Event multiplicity = 170
 - R : Total interaction rate = 15 kHz

- b : 1/driftlength
- $c \cdot e$: 0 for all the plots in next few slides
- Radial dependence (d) = 2 & $f_d = 1$

3.2. Scaling STAR observations to ALICE expectations

The normalized distribution of charge density used in the STAR TPC to correct for the space-charge effect is:

$$\rho(r, z) = \frac{(L - z)}{L} \frac{(r_O^2 - r_I^2)}{\log(r_O/r_I)} \frac{0.01}{1.5 \cdot 10^6} \frac{IR}{r^2} \quad (6)$$

where $r_O=200\text{cm}$ and $r_I=47.9\text{cm}$ are the outer and inner radii (STAR TPC dimensions). The empirical factor which corresponds roughly to an interaction rate (IR) of 15 kHz for Au-Au collisions at a center of mass energy of 200 GeV is then:

$$F_E = \frac{(r_O^2 - r_I^2)}{\log(r_O/r_I)} \frac{0.01}{1.5 \cdot 10^6} = 1.76 \cdot 10^{-2}$$

- So for STAR the empirical factor should look like :
 $F_{E,S} = (\text{Min bias multiplicity in STAR}) / F_E$, where $F_E = 1.76 \text{ e-02}$
 $= 340. / 1.76\text{e-02} = 19318.2$

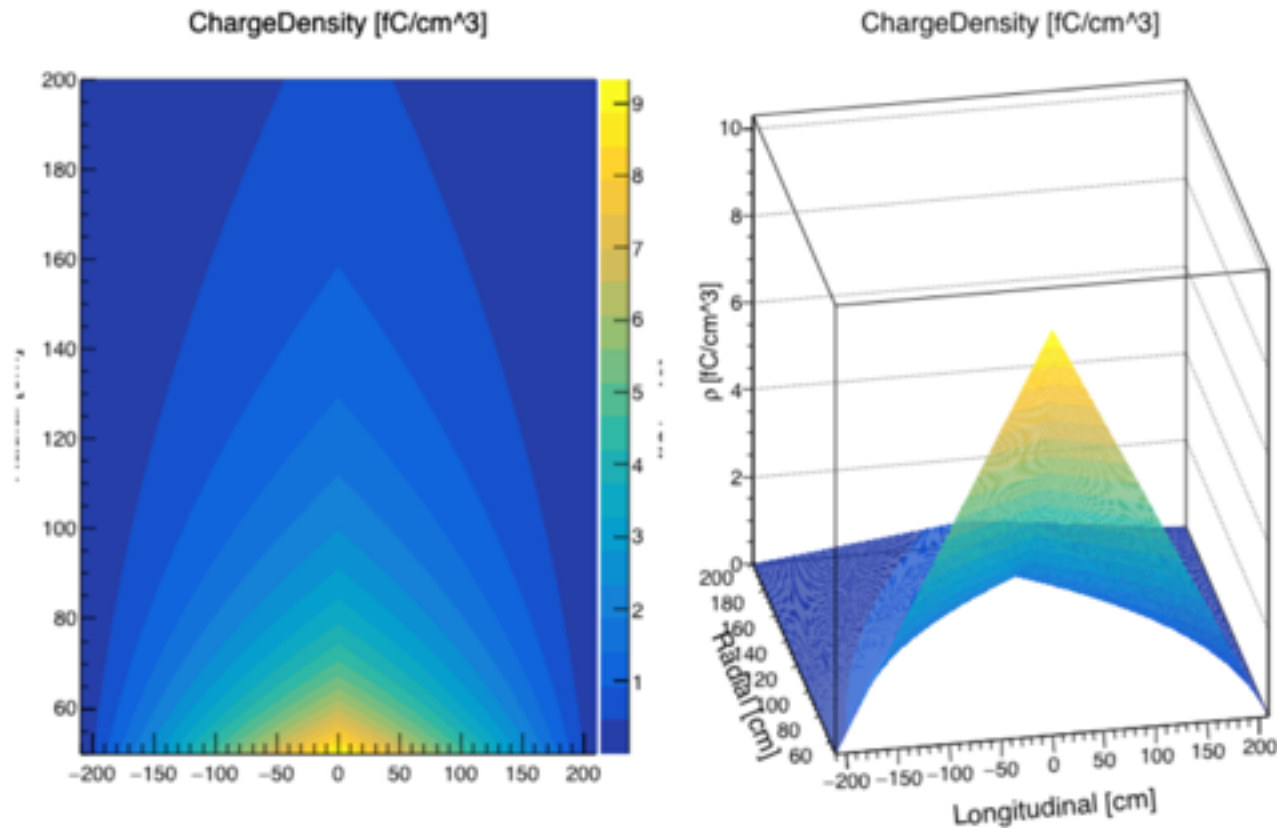
Using formula (6), we can calculate an empirical factor for the ALICE TPC where we include a scaling factor for the min.bias multiplicities (with $M_{mb,S} = 127$ for the top 80 % within STAR) and the design scaling factor F_D from Tab. 4:

$$F_{E,A} = (F_E \cdot F_D / M_{mb,S})^{-1} = 76628 .$$

The complete empirical formula can be written as:

Few cases of STAR charge density by changing the gas factor and keeping $c \cdot \epsilon_s = 0$

Gas Factor [G] = 1.0



$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

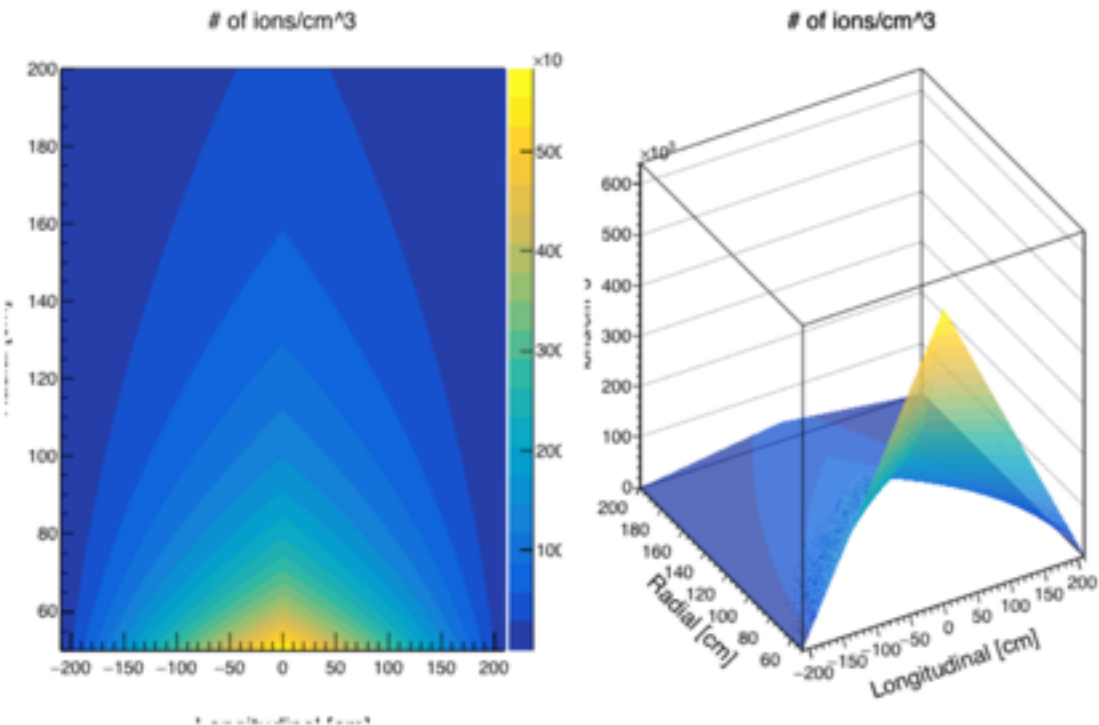
$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

STAR values

Charge density in new simulation
using Toy model $\sim 8.5 \text{ e-14 C/cm}^3$
 $\sim 5.3\text{e+05 qe/cm}^3$

STAR number of ions density with gas factor [G] = 1.0

New simulation



Number of ions per cm³ using new simulation $\sim 5.3 \times 10^5$ qe/cm³

STAR estimate

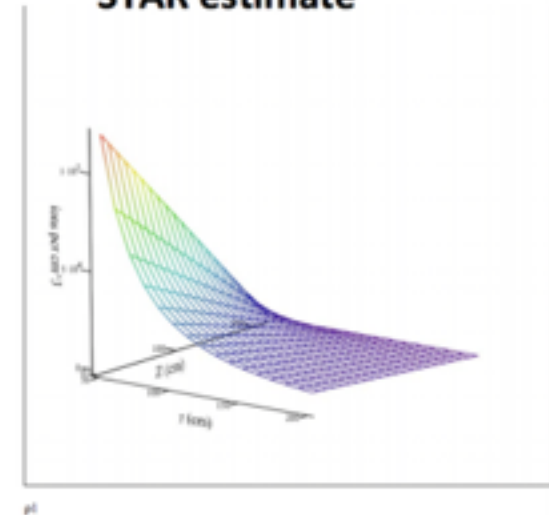


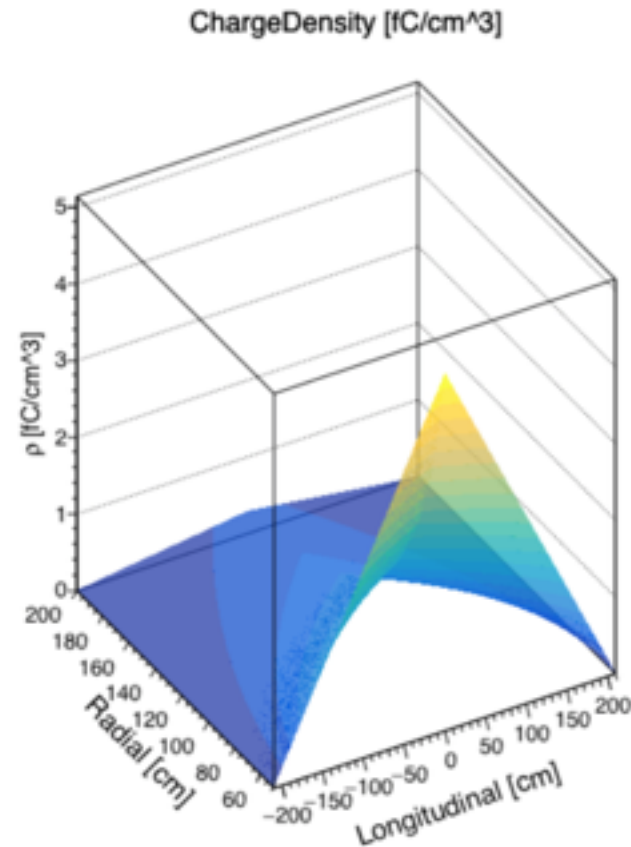
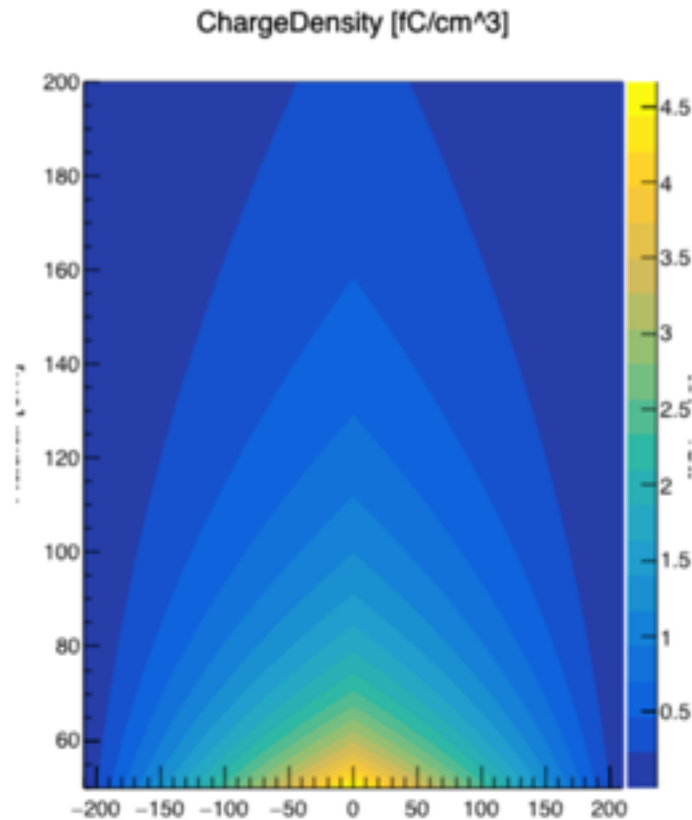
Fig. 2 Steady state positive ion density as a function of r and z in the TPC volume for RHIC II predicted AuAu luminosity. This is the positive ion density that produced the distortion shown in Fig. 1

STAR values

$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

STAR charge density with gas factor [G] = 0.5



STAR values

$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

Charge density using new simulation
~ 4.5 e-14 C/cm³

STAR number of ions density with gas factor [G] = 0.5

New simulation

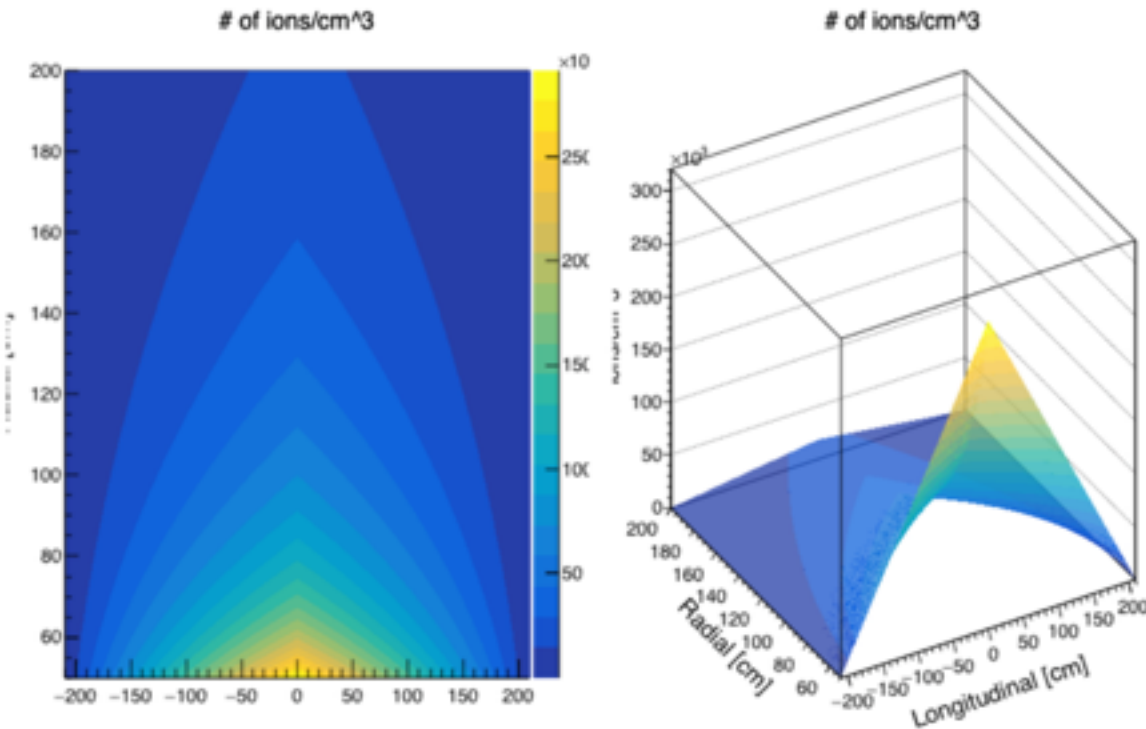


Figure 1: Ion density distribution in the TPC volume.

Charge density using new simulation
 $\sim 2.8 \times 10^5 \text{ qe/cm}^3$

STAR estimate

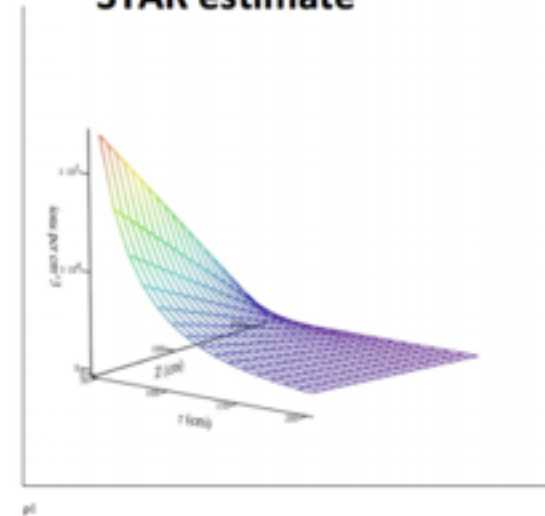


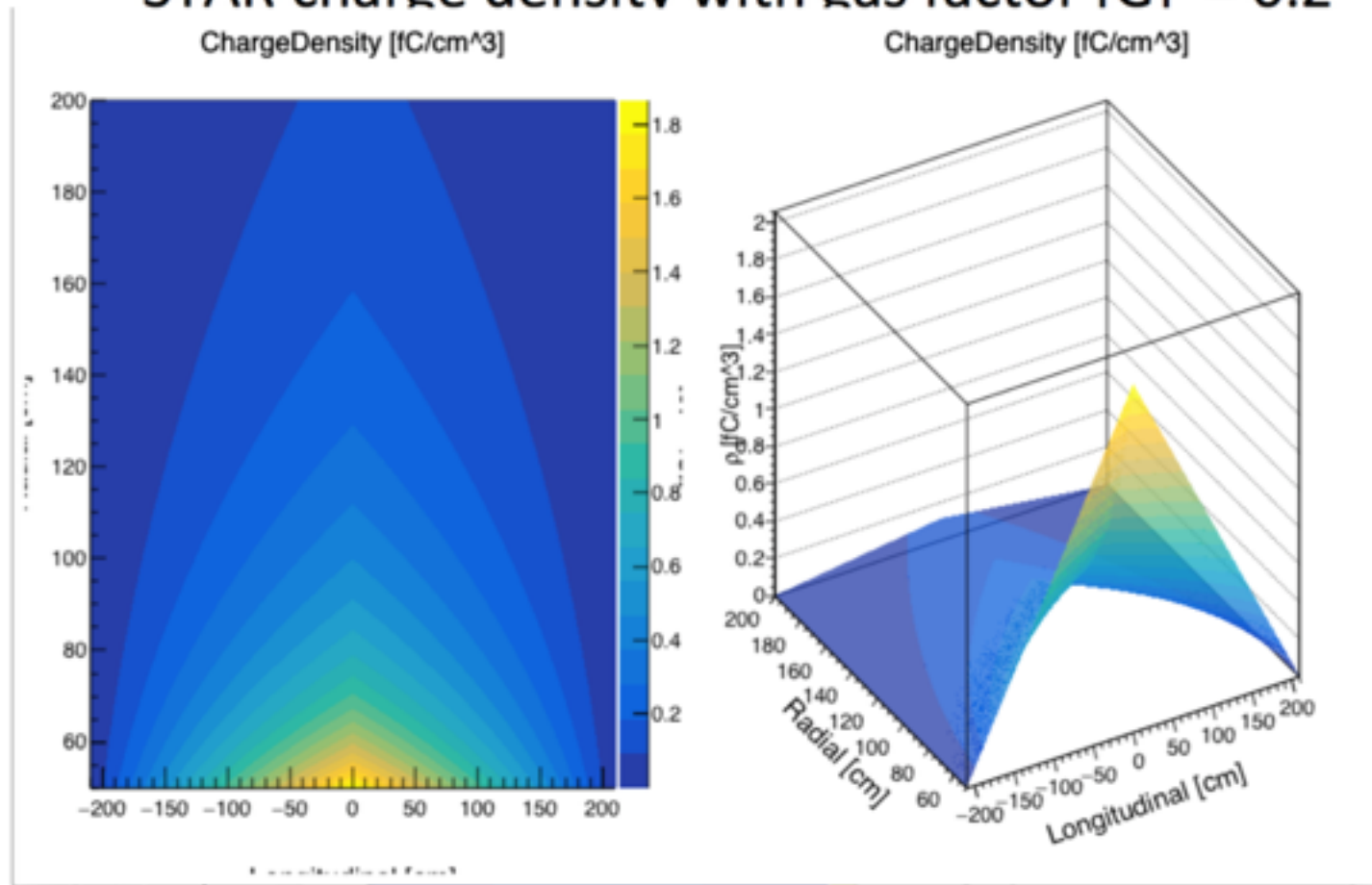
Fig. 2 Steady state positive ion density as a function of r and z in the TPC volume for RHIC B predicted AuAu luminosity. This is the positive ion density that produced the distortion shown in Fig. 1

STAR values

$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

STAR charge density with gas factor [G] = 0.2



STAR values

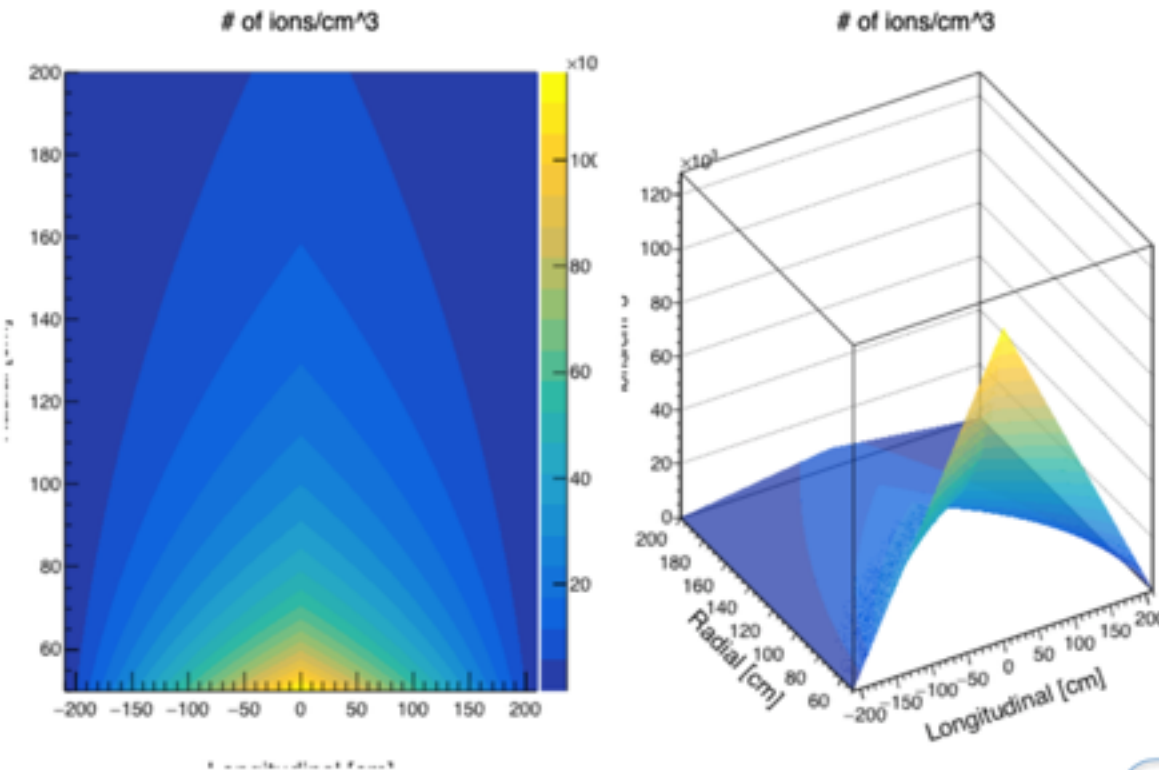
$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

Charge density using new simulation
 $\sim 1.8 \text{ e-14 C/cm}^3$

STAR number of ions density with gas factor [G] = 0.2

New simulation



STAR estimate

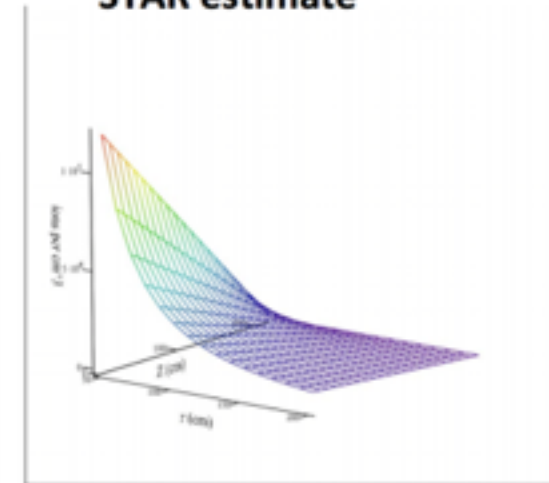


Fig. 2 Steady state positive ion density as a function of r and z in the TPC volume for RHIC predicted AuAu luminosity. This is the positive ion density that produced the distortion shown in Fig. 1

STAR values

$$\rho(50\text{cm}, 0\text{cm}) = 1.9 \times 10^{-14} \frac{\text{coul}}{\text{cm}^3}$$

$$\rho(50\text{cm}, 0\text{cm}) = 1.2 \times 10^5 \frac{\text{qe}}{\text{cm}^3}$$

Charge density using new simulation
 $\sim 1.12 \text{ e}+05 \text{ qe/cm}^3$

Setting gas factor [G] between 0.2 and 0.5 gives almost same estimate of space charge as done by STAR for STAR TPC

Space charge density in the TPC volume

Toy model:

$$\rho(\mathbf{r}_-, \mathbf{z}_-) := A \left(\frac{1 - b \mathbf{z} + c \epsilon}{f_d r^d} \right)$$

1. Proportionality to the primary ionisation (i.e. local track density in a collision) r^{-2} dependence and z drift velocity
2. Back flow dependence as CTE in z direction

Space charge density in the TPC volume

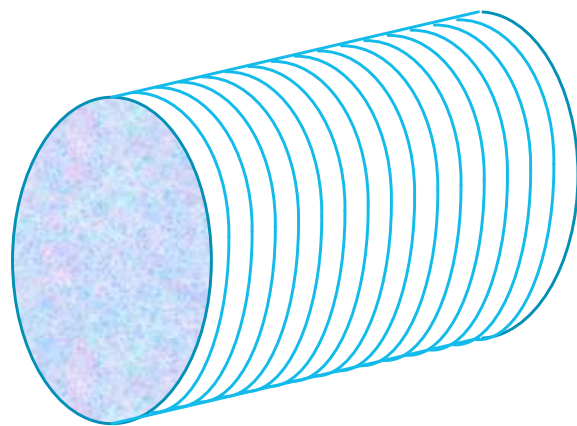
$$\rho(r_-, z_-) := A \left(\frac{1 - b z + c \epsilon}{f_d r^d} \right)$$

- $A = [G] \times [M] \times [R] \times [e_0] / 76628$ [in C/m]
 - e_0 ($=8.85e-12$): vacuum permittivity [in As/(Vm)]
 - G ($=1$): gas factor (prim ioniz. / drift velocity)
 - M ($=950$): nominal event multiplicity
 - R ($=5e4$): total interaction rate [in Hz]
- b ($=1/2.5$): $1/\text{DriftLength}$ [in 1/m]
- $c \cdot e$ ($=2/3 \cdot 20$)
- d ($=2$ for STAR $f_d=1$; $=1.5$ for ALCE)

All gas parameters are
embedded in $G/76628$

Factorization of the Space Charge Problem

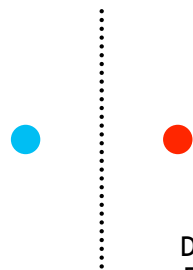
Cylinder with graded potentials and space charge in the volume



Point + Sheet

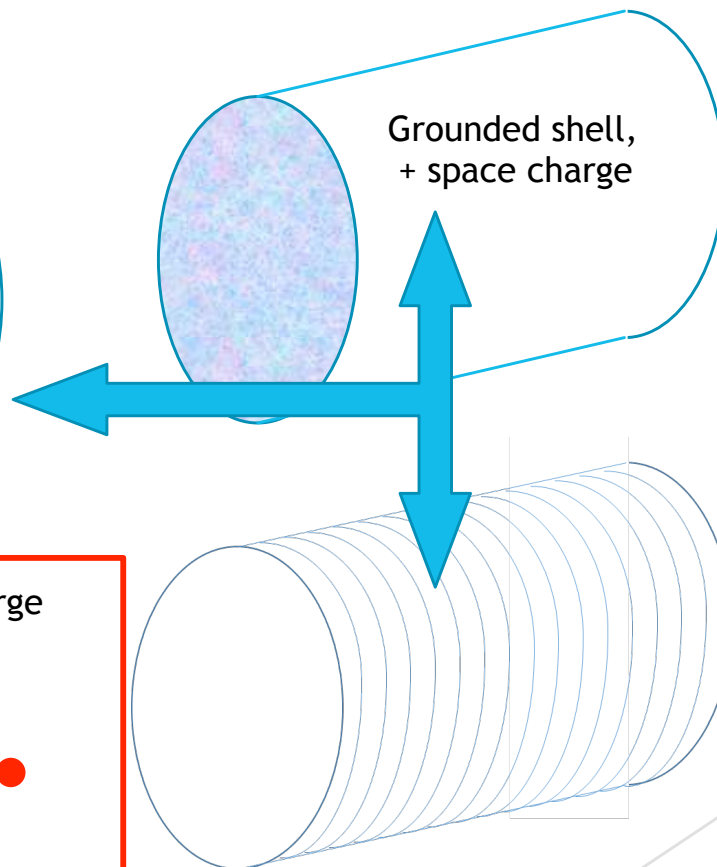


Image Charge



Dipole Field!

Grounded shell, + space charge



Graded potentials, no charge

- ▶ Graded field cage field determined by ANSYS or COLSOL finite element calculations.

- ▶ Grounded shell solved using Greene's theorem

$$\Delta G(r, r_{\downarrow ch}) = \delta(r - r_{\downarrow ch})$$

$$E_{\downarrow ch}(r, r_{\downarrow ch}) = \nabla G(r, r_{\downarrow ch})$$

$$E = \int \rho(r_{\downarrow ch}) E_{\downarrow ch}(r, r_{\downarrow ch}) dV_{\downarrow ch}$$

Carlos

Tom

Basic Approach to Solving the Cylinder

- The problem at hand is this: $\Delta G(\vec{x}; \vec{x}') = -\delta(\vec{x} - \vec{x}'),$ (5.13)

$$\left[\frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \phi^2} + \frac{\partial^2}{\partial z^2} \right] G(r, \phi, z; r', \phi', z') = -\frac{\delta(r-r')}{r} \delta(\phi-\phi') \delta(z-z'). \quad (5.14)$$

- Our solution begins with solving the homogeneous equation to provide a basis set of functions for the full solution: $\Delta \Phi = 0, \quad \left(\frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \phi^2} + \frac{\partial^2}{\partial z^2} \right) \Phi(r, \phi, z) = 0, \quad \Phi(r, \phi, z) = R(r)\Phi(\phi)Z(z).$

Periodicity set $m=0,1,2,3,\dots$ $\Phi_m(\phi) = C_m e^{im\phi} = A_m \cos(m\phi) + B_m \sin(m\phi) \quad \text{with } m \in \mathbb{Z}.$

$$\frac{R_{rr}}{R} + \frac{1}{r} \frac{R_r}{R} - \frac{m^2}{r^2} = -\frac{Z_{zz}}{Z} = \begin{cases} -\beta^2, & \text{case I;} \\ \beta^2, & \text{case II.} \end{cases}$$

Solution without boundary conditions applied:

$$Z_m(z) = C_m \cosh(\beta z) + D_m \sinh(\beta z),$$

$$R_m(r) = E_m J_m(\beta r) + F_m Y_m(\beta r).$$

Constants formulated to explicitly vanish at $r=a$

$$R_{mn}(r) = Y_m(\beta_{mn}a)J_m(\beta_{mn}r) - J_m(\beta_{mn}a)Y_m(\beta_{mn}r).$$

Vanishing at $r=b$ forces β to become discrete.

Finishing the solution

- Once the solutions to the homogeneous equation are known, we express the Dirac delta function in this basis:

$$\delta(\phi - \phi') = \frac{1}{2\pi} \sum_{m=-\infty}^{\infty} e^{im(\phi - \phi')} = \frac{1}{2\pi} \sum_{m=0}^{\infty} (2 - \delta_{m0}) \cos[m(\phi - \phi')],$$

$$\frac{\delta(r - r')}{r} = \sum_{n=1}^{\infty} \frac{R_{mn}(r) R_{mn}(r')}{N_{mn}^2} \quad \text{with} \quad N_{mn}^2 = \int_a^b R_{mn}^2(r) r dr,$$

$$m = 0, 1, 2, \dots$$

- After which the solution is readily obtained:

$$G(r, \phi, z, r', \phi', z') = \frac{1}{2\pi} \sum_{m=0}^{\infty} \sum_{n=1}^{\infty} (2 - \delta_{m0}) \cos[m(\phi - \phi')] \frac{R_{mn}(r) R_{mn}(r')}{N_{mn}^2} \frac{\sinh(\beta_{mn} z_{<}) \sinh(\beta_{mn} (L - z_{>}))}{\beta_{mn} \sinh(\beta_{mn} L)},$$

- Although the solution is correct, it is not assured to be readily convergent.
- Rossegger used three independent basis sets to obtain stable, differentiable, convergent solutions for the r , ϕ , and z components of the field:

$\frac{\partial}{\partial z} G(r, \phi, z, r', \phi', z') = \frac{1}{2\pi} \sum_{m=0}^{\infty} \sum_{n=1}^{\infty} (2 - \delta_{m0}) \cos[m(\phi - \phi')] \frac{R_{mn}(r) R_{mn}(r')}{N_{mn}^2} \frac{\partial}{\partial z} \left(\frac{\sinh(\beta_{mn} z_{<}) \sinh(\beta_{mn} (L - z_{>}))}{\beta_{mn} \sinh(\beta_{mn} L)} \right),$ <p style="text-align: center;">(5.64)</p> <p>with $\frac{\partial}{\partial z} (\sinh(\beta_{mn} z_{<}) \sinh(\beta_{mn} (L - z_{>}))) =$</p> $= \begin{cases} \beta_{mn} \cosh(\beta_{mn} z) \sinh(\beta_{mn} (L - z')), & \text{for } 0 \leq z < z' \leq L, \\ -\beta_{mn} \cosh(\beta_{mn} (L - z)) \sinh(\beta_{mn} z'), & \text{for } 0 \leq z' < z \leq L. \end{cases}$	$\frac{\partial}{\partial r} G(r, \phi, z, r', \phi', z') = \frac{1}{\pi L} \sum_{m=0}^{\infty} \sum_{n=1}^{\infty} (2 - \delta_{m0}) \cos[m(\phi - \phi')] \sin(\beta_n z) \sin(\beta_n z') \frac{\partial}{\partial r} \left(\frac{R_{mn1}(r_{<}) R_{mn2}(r_{>})}{I_m(\beta_n a) K_m(\beta_n b) - I_m(\beta_n b) K_m(\beta_n a)} \right),$ <p style="text-align: center;">(5.65)</p> <p>with $\frac{\partial}{\partial r} (R_{mn1}(r_{<}) R_{mn2}(r_{>})) = \begin{cases} R'_{mn}(a, r) R_{mn2}(r'), & \text{for } a \leq r < r' \leq b, \\ R_{mn1}(r') R'_{mn}(b, r), & \text{for } a \leq r' < r \leq b, \end{cases}$</p> <p>wherein $R'_{mn}(s, t)$ is</p> $R'_{mn}(s, t) = \frac{\beta_n}{2} (K_m(\beta_n s) (I_{m-1}(\beta_n t) + I_{m+1}(\beta_n t)) + I_m(\beta_n s) (K_{m-1}(\beta_n t) + K_{m+1}(\beta_n t))).$	$\frac{\partial}{\partial \phi} G(r, \phi, z, r', \phi', z') = \frac{1}{L} \sum_{k=1}^{\infty} \sum_{n=1}^{\infty} \sin(\beta_n z) \sin(\beta_n z') \frac{R_{nk}(r) R_{nk}(r')}{N_{nk}^2} \frac{\partial}{\partial \phi} \left(\frac{\cosh[\mu_{nk}(\pi - \phi - \phi')]}{\mu_{nk} \sinh(\pi \mu_{nk})} \right)$ <p style="text-align: center;">(5.66)</p> <p>with $\frac{\partial}{\partial \phi} (\cosh[\mu_{nk}(\pi - \phi - \phi')]) =$</p> $= \begin{cases} -\mu_{nk} \sinh[\mu_{nk}(\pi - (\phi - \phi'))], & \text{for } 0 \leq \phi' < \phi \leq 2\pi \\ \mu_{nk} \sinh[\mu_{nk}(\pi - (\phi' - \phi))], & \text{for } 0 \leq \phi < \phi' \leq 2\pi \end{cases}$
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Langevin Eq:

charge of the drifting particle

Friction ($K > 0$)

$$m \frac{d \vec{u}}{dt} = q e \vec{E} + q e \left[\vec{u} \times \vec{B} \right] - K \vec{u}$$

drift velocity

EB force

Solution:

$t \gg m/K$ Adiabatic approx.

$\frac{d \vec{u}}{dt} = 0$ Steady state

$$\vec{u} = \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E} + \omega \tau (\hat{E} \times \hat{B}) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B} \right]$$

scalar mobility of the electric field

$$\mu = \frac{q e}{K}$$

mean interaction time between drifting electrons and atoms from the gas

cyclotron frequency for electron

$$\omega \tau = q \mu B$$

Drift velocity in cartesian coordinates

$$\begin{aligned}u_x &= \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_x + \omega \tau (\hat{E}_y \hat{B}_z - \hat{E}_z \hat{B}_y) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_x \right] \\u_y &= \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_y + \omega \tau (\hat{E}_z \hat{B}_x - \hat{E}_x \hat{B}_z) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_y \right] \\u_z &= \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_z + \omega \tau (\hat{E}_x \hat{B}_y - \hat{E}_y \hat{B}_x) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_z \right]\end{aligned}$$

We can compute the path integral of the drifting electron

$$\delta_x = \int u_x \, d\mathbf{t} = \int \frac{u_x}{u_z} \frac{d\mathbf{z}}{d\mathbf{t}} \, d\mathbf{t} = \int \frac{u_x}{u_z} \, d\mathbf{z}$$

$$\delta_y = \int \frac{u_y}{u_z} \, d\mathbf{z}$$

$$\delta_z = \int \frac{u_z}{u_0} \, d\mathbf{z}$$

TPC case: $E_z \gg E_x, E_y$ $B_z \gg B_x, B_y$

$$u_x = \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_x + \omega \tau (\hat{E}_y \hat{B}_z - \hat{E}_z \hat{B}_y) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_x \right]$$

$$u_y = \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_y + \omega \tau (\hat{E}_z \hat{B}_x - \hat{E}_x \hat{B}_z) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_y \right]$$

$$u_z = \frac{\mu \left| \vec{E} \right|}{1 + \omega^2 \tau^2} \left[\hat{E}_z + \omega \tau (\hat{E}_x \hat{B}_y - \hat{E}_y \hat{B}_x) + \omega^2 \tau^2 (\hat{E} \cdot \hat{B}) \hat{B}_z \right]$$

Second order expansion:

$$\hat{E}_x \approx \frac{\hat{E}_x}{E_z}$$

$$\hat{E}_z \approx 1 - \frac{1}{2} \hat{E}_x^2 - \frac{1}{2} \hat{E}_y^2$$

$$\frac{u_x}{u_z} = \frac{1}{1 + \omega^2 \tau^2} \frac{E_x}{E_z} + \frac{\omega \tau}{1 + \omega^2 \tau^2} \frac{E_y}{E_z} - \frac{\omega \tau}{1 + \omega^2 \tau^2} \frac{B_y}{B_z} + \frac{\omega^2 \tau^2}{1 + \omega^2 \tau^2} \frac{B_x}{B_z}$$

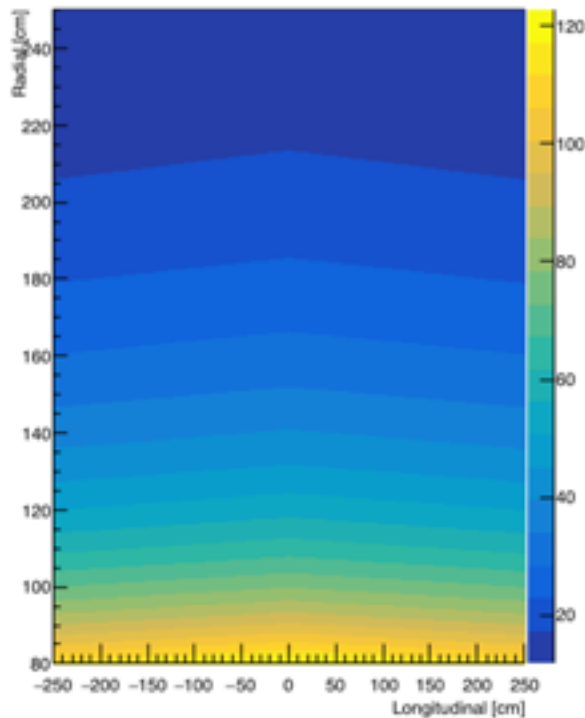
$$\frac{u_y}{u_z} = \frac{1}{1 + \omega^2 \tau^2} \frac{E_y}{E_z} - \frac{\omega \tau}{1 + \omega^2 \tau^2} \frac{E_x}{E_z} + \frac{\omega \tau}{1 + \omega^2 \tau^2} \frac{B_x}{B_z} + \frac{\omega^2 \tau^2}{1 + \omega^2 \tau^2} \frac{B_y}{B_z}$$

Initial Charge Density

ALICE

Radial dependence set at 2
Gas factor at 1.0/76628.0
Multiplicity at 900
DC Rate at 50kHz
BackFlow at 20 (=1.0%2000)

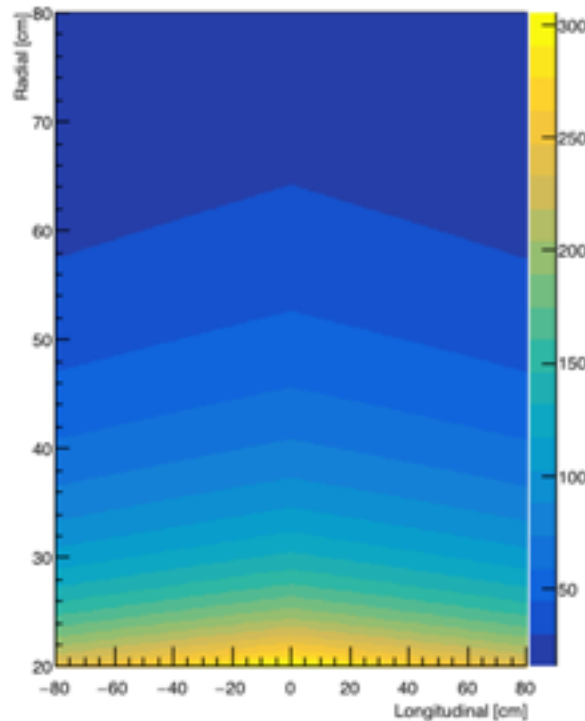
ChargeDensity [fC/cm³]



sPHENIX20

Radial dependence set at 2
Gas factor at 1.0/76628.0
Multiplicity at 450
DC Rate at 50kHz
BackFlow at 6 (=0.3%2000)

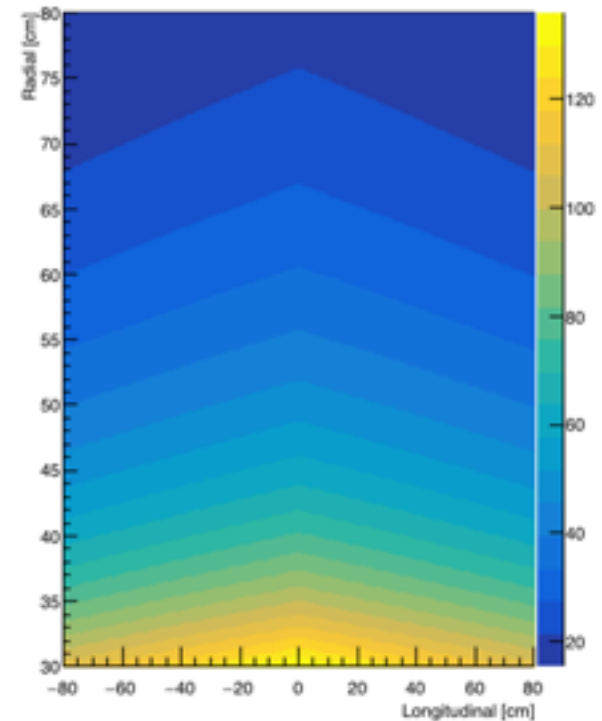
ChargeDensity [fC/cm³]



sPHENIX30

Radial dependence set at 2
Gas factor at 1.0/76628.0
Multiplicity at 450
DC Rate at 50kHz
BackFlow at 6 (=0.3%2000)

ChargeDensity [fC/cm³]



Induced Electric Field

ALICE

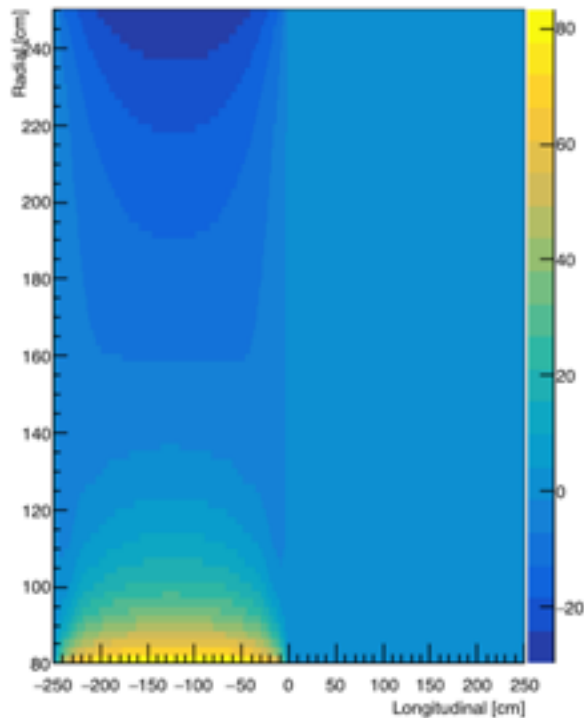
Grid size:

Rad = 2.13 cm

Phi = 360 deg

Lon = 2 cm

Er [V/cm]



sPHENIX20

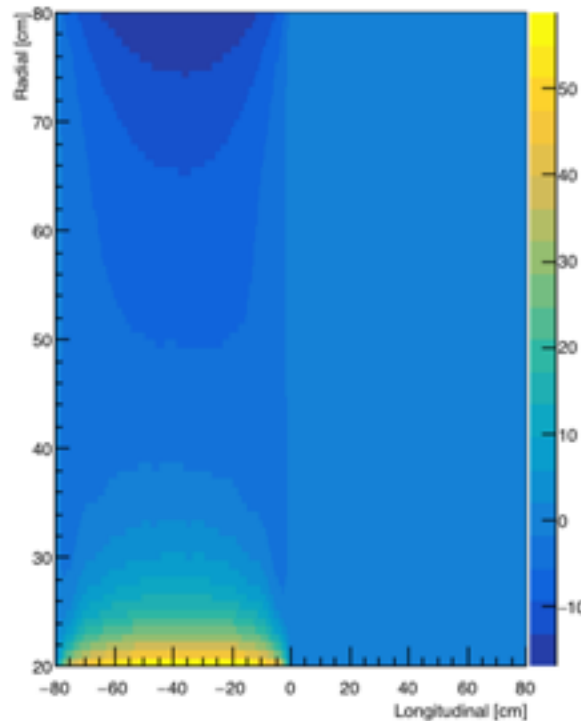
Grid size:

Rad = 0.75 cm

Phi = 360 deg

Lon = 0.64 cm

Er [V/cm]



sPHENIX30

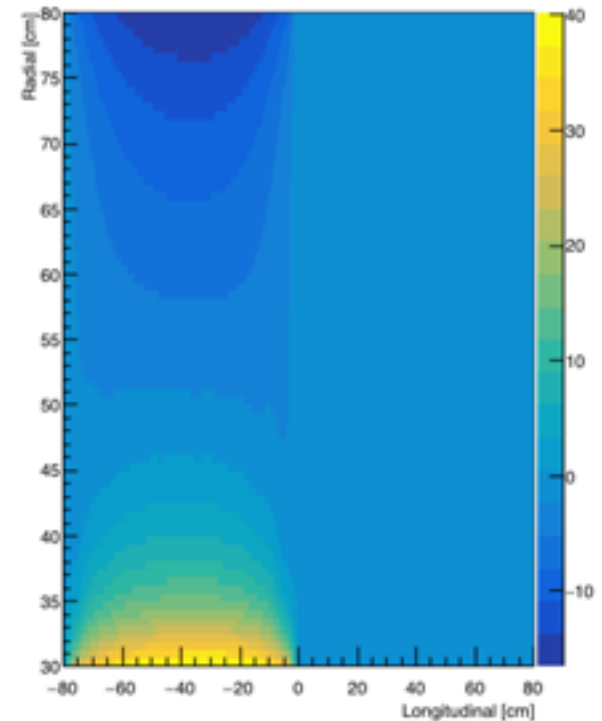
Grid size:

Rad = 0.63 cm

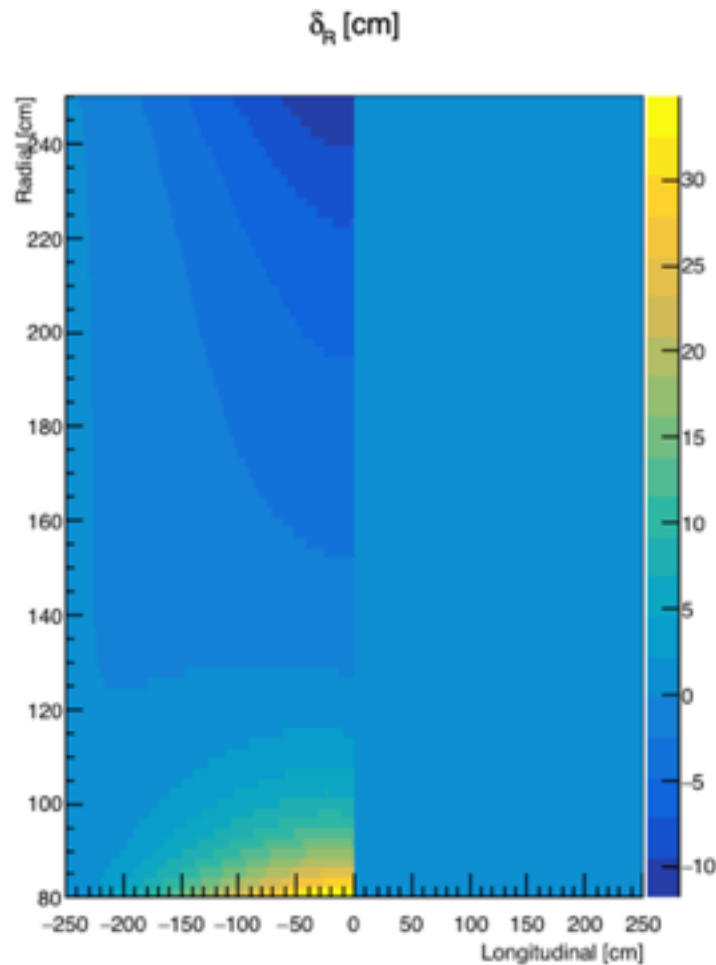
Phi = 360 deg

Lon = 0.64 cm

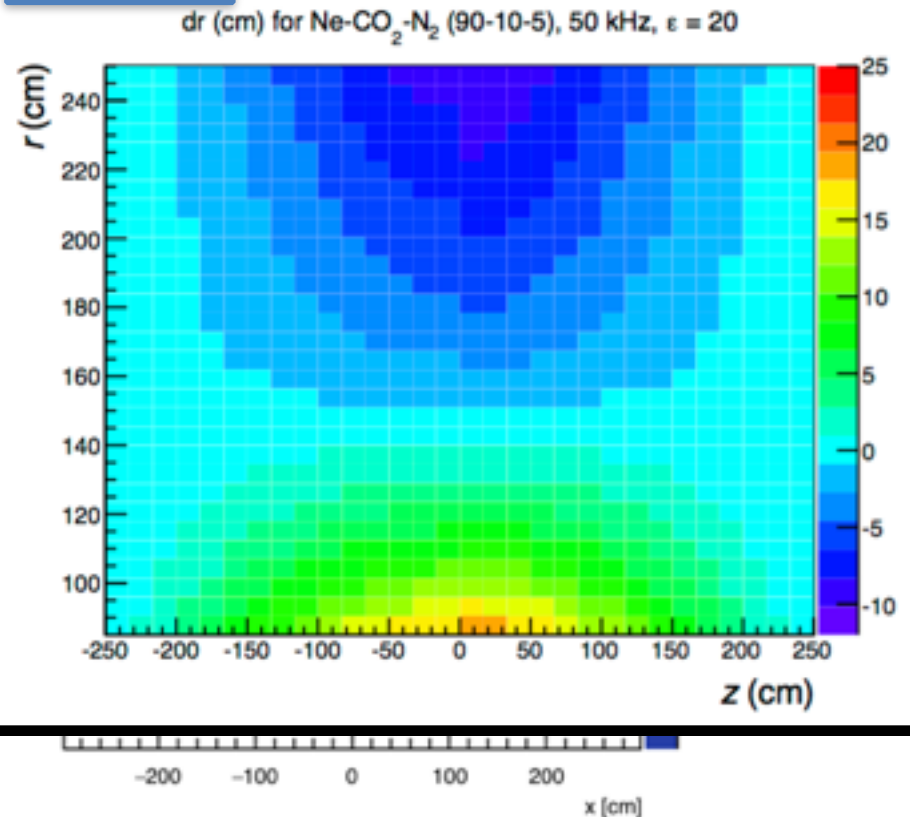
Er [V/cm]



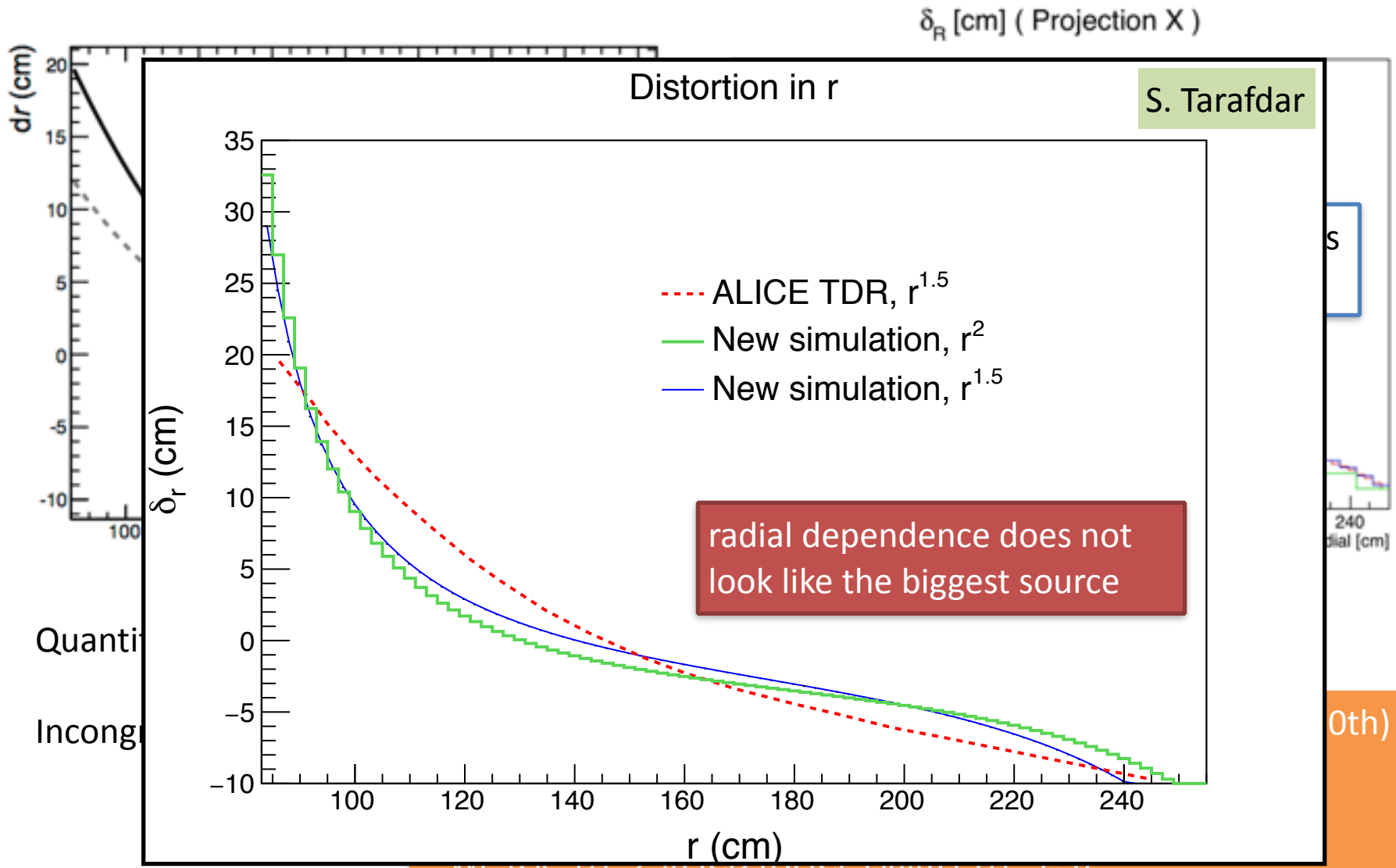
Comparing with ALICE TDR (1/2)



ALICE TDR



Comparing with ALICE TDR (2/2)



- ...?

Traces to pairs

- Ingredients
 - DeltaE for the total track length
 - DeltaE to N ionised electrons

Gas	Ratio	Density*10 ³ (g/cm ³)	Radiation Length (m)	N _p (cm ⁻¹)	N _e (cm ⁻¹)
Ne-CH ₄	90-10	0.881	361.8	13.45	44
	80-20	0.862	380.4	14.9	45
	70-30	0.843	401	16.35	46
Ne-C ₂ H ₆	90-10	.0944	344	14.9	49.8
	80-20	0.988	343.9	17.8	56.6
	70-30	1.032	343.4	20.7	63.4
Ne-iC ₄ H ₁₀	90-10	1.06	312	19.2	58.2
	80-20	1.23	285	26.4	73.4
	70-30	1.4	262	33.6	88.6
Ne-CO ₂	90-10	1	317	14.35	47.8
	80-20	1.12	293	16.7	52.6
	70-30	1.22	272	19	57.4
Xe-CH ₄	90-10	5.34	16.6	42.25	281.6
	80-20	4.83	18.6	40.5	256.2
	70-30	4.31	21.2	38.75	230.8
Xe-C ₂ H ₆	90-10	5.4	16.6	43.7	287.4
	80-20	4.95	18.5	43.4	267.8
	70-30	4.5	21	43.1	248.2
Xe-iC ₄ H ₁₀	90-10	5.53	16.5	48	295.8
	80-20	5.2	18.3	52	284.6
	70-30	4.87	20.6	56	273.4
Xe-CO ₂	90-10	5.47	16.5	43.15	285.4
	80-20	5.1	18.4	42.3	263.8
	70-30	4.69	20.7	41.45	242.2

Table 1. (Continued) Parameters of some gas and gas mixtures.

For the moment, I parametrised the number of Nt per cm as cte from this table